

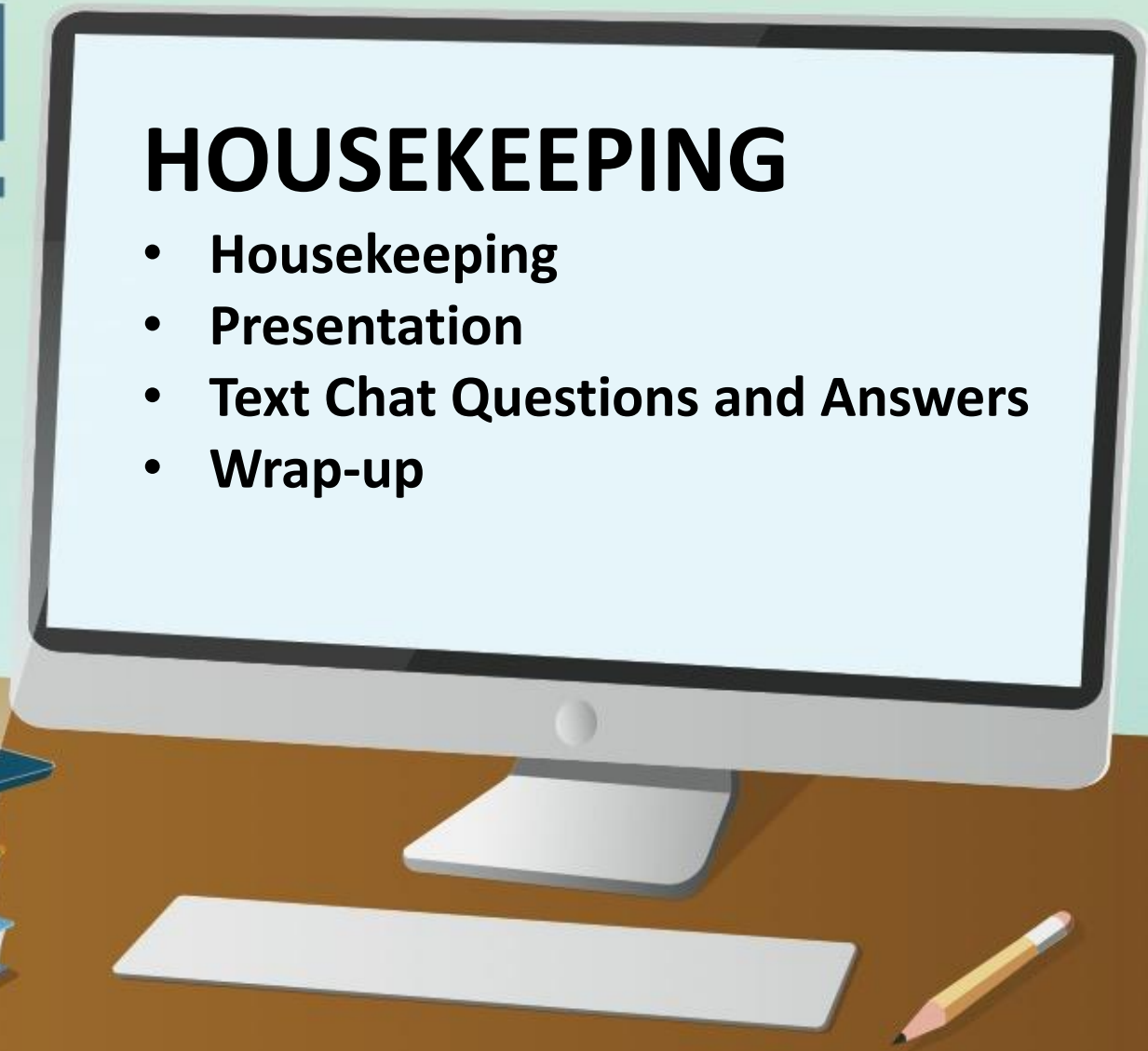
# Digital Power Regulation Solutions

Instructor:  
Tom Spohrer,  
Product Marketing Manager,  
MCU16 Division, Microchip Technology, Inc.



## HOUSEKEEPING

- Housekeeping
- Presentation
- Text Chat Questions and Answers
- Wrap-up



# Agenda

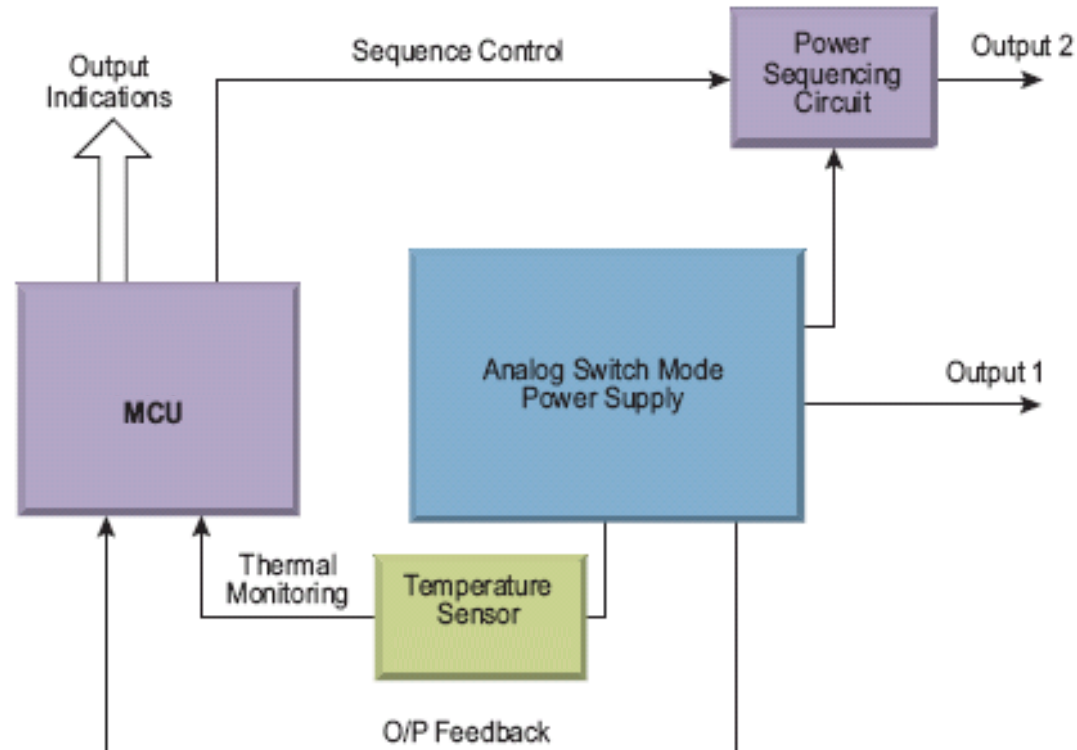
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- **Review the Levels of Digital Integration**
  - **Benefits of Full Digital Control**
  - **Digital Controller Basics**
    - Analog SMPS and Digital SMPS Implementations
  - **The Digital PID**
    - The Mathematics, Generating the Coefficients, DSC Digital PID Implementation
  - **Typical DSC Firmware Architecture**
  - **Other Digital Compensator Types**
  - **Advanced Digital Control**
    - Adaptive, Non-linear, and Predictive algorithms
  - **Additional Resources**
    - App Notes, Libraries, Digital Compensator Design Tool, Workshops
-

# Levels of Digital Integration

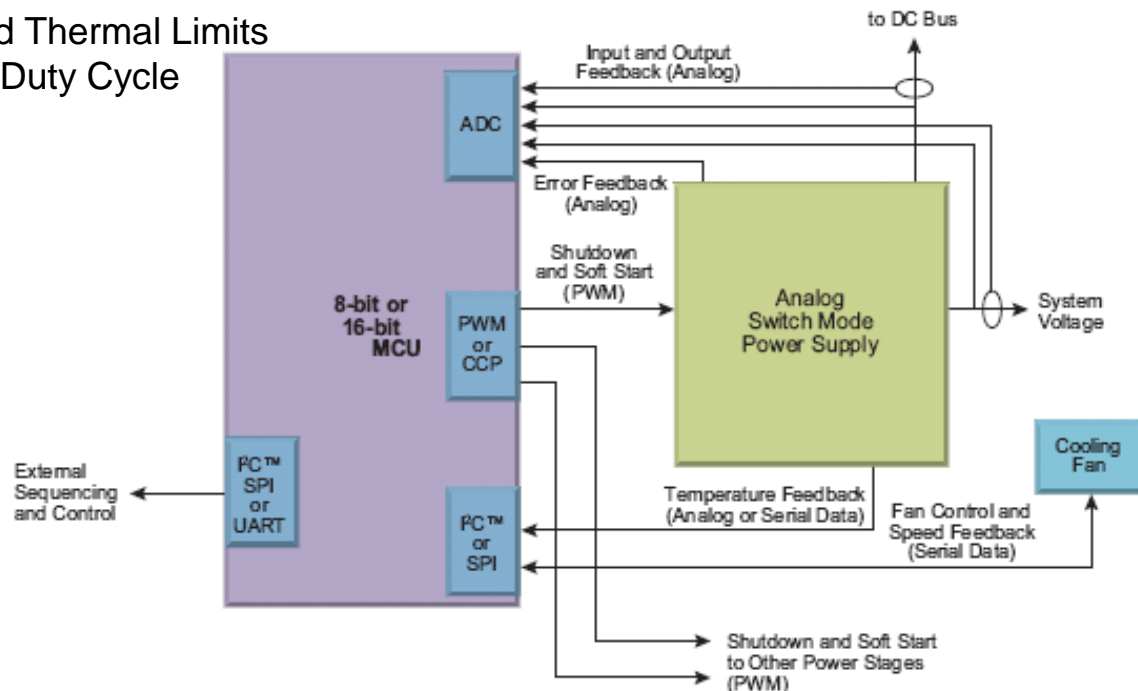
- **Level 1: Control improves traditional analog power design**

- Soft-start and Power Sequencing
- Voltage and Temperature Monitoring
- Communication and Data Logging



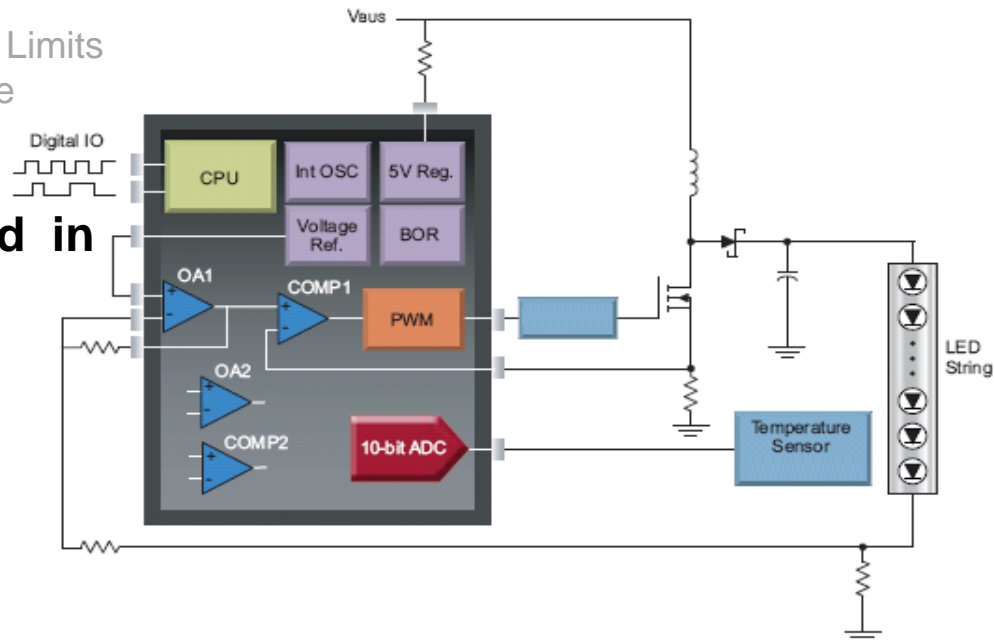
# Levels of Digital Integration

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- **Level 2: MCU controls reference signals for the PWM Controller**
  - Indirectly Set Voltage, Current and Thermal Limits
  - Determine PWM Period and Max Duty Cycle
  - Self-calibration



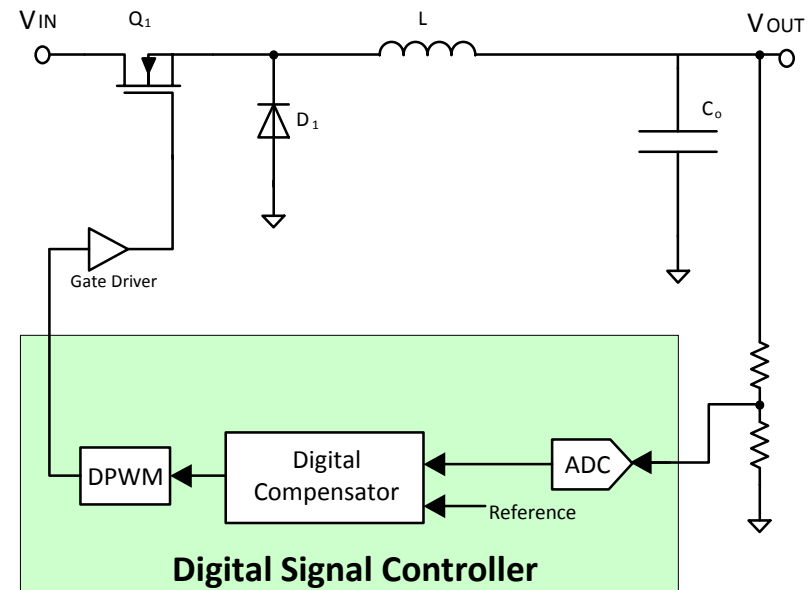
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  - Micro Controls the Feedback and PWM



# Levels of Digital Integration

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- **Level 3: Analog functions integrated in MCU and can be reconfigured for changing load conditions**
  - Micro Controls the Feedback and PWM
- **Level 4: Analog feedback is replaced with complete digital DSP-based control**
  - PID, 2P2Z, 3P3Z Algorithms with Voltage or Current Mode Control



# Technical Advantages of Digital Control

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- Software-driven controllers can implement any topology
- Non-linear, predictive, and adaptive control techniques can be implemented for highest efficiency across widely varying load and environmental conditions
- Change topology “On-the-Fly”: e.g. multi-phase to single phase at low-load to optimize efficiency
- Minimize over-specification of magnetic components because DSC provides tighter tolerance than passive Rs & Cs
- Reduced BOM costs
- Fewer components result in higher power densities and higher reliability





# Business Advantages of Digital Control

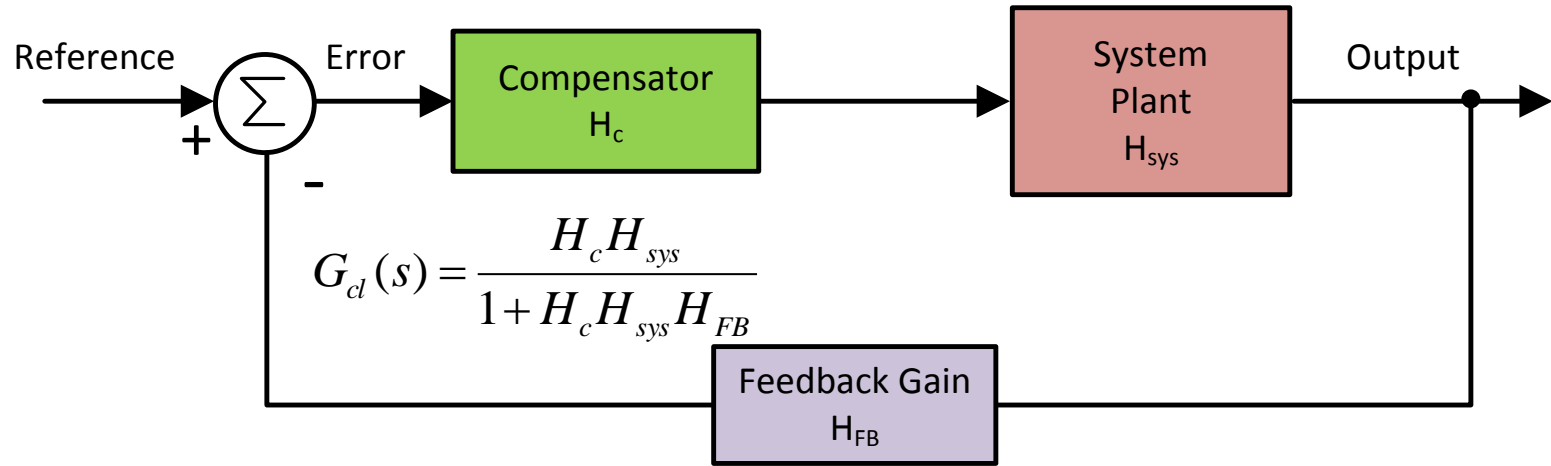
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- IP belongs to PS vendor & resides in secured firmware
- Fewer hardware platforms support more products
- Easily update software to meet changing customer needs
- Improved self-test capability simplifies product testing
- Component tolerance & drift reduced:  
(Eliminate “Over specified” components)
- Restrict products from operating beyond specification
- Log any misuse in the advent of warranty return



# Controller Basics

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**Reference:** This is the desired set-point we want the Output to follow

**Error:** Calculation of (Reference – Feedback), this is the value the compensator acts upon

**Compensator:** Digital compensator (PID, 2P2Z, 3P3Z, or 4<sup>th</sup> order, etc.)

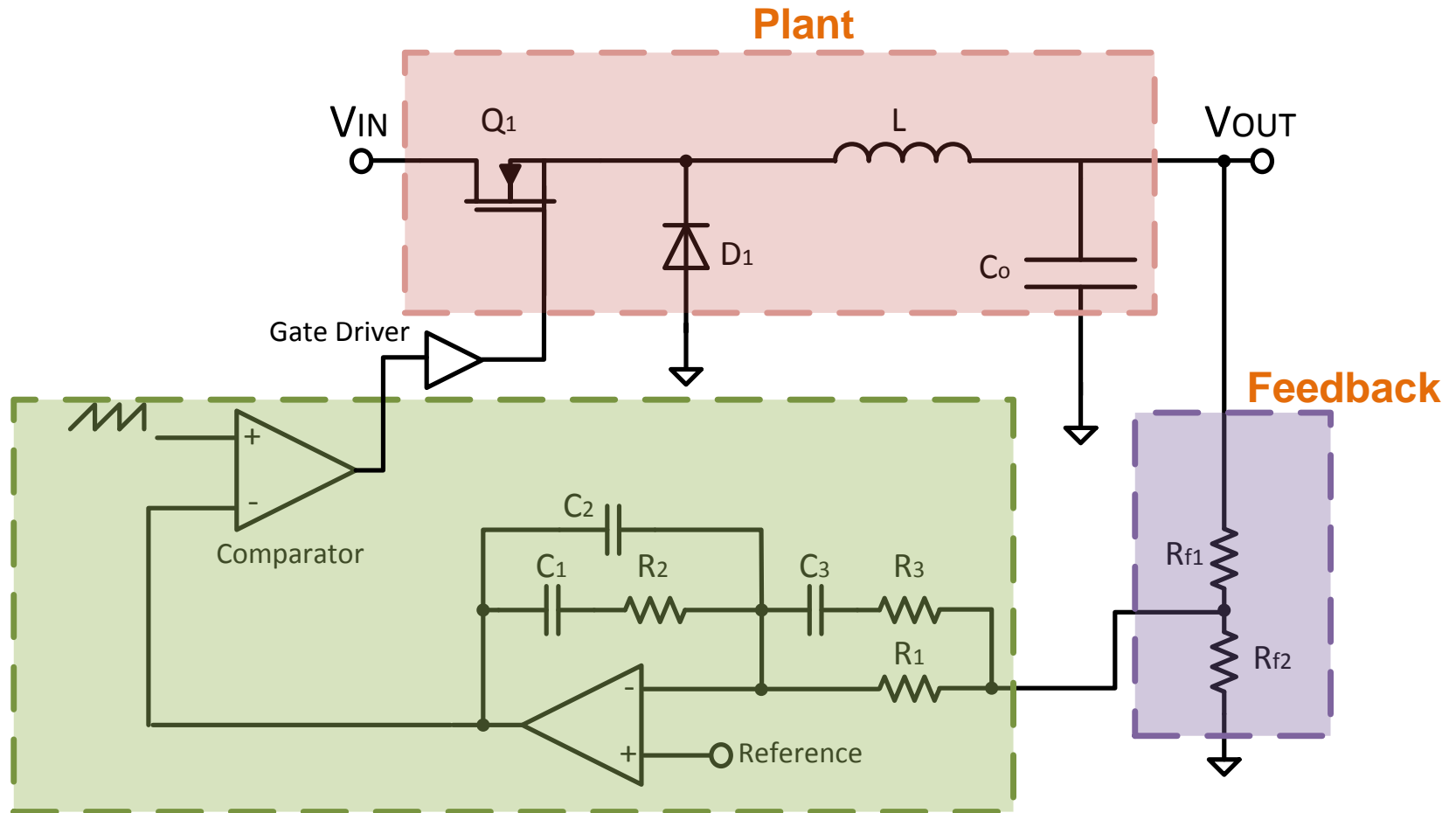
**System:** This is the System/Plant/Power stage being controlled (SMPS, Motor, Actuator, etc)

**Output:** For our purposes this will be Voltage or Current

**Feedback:** The measurement of the output signal level

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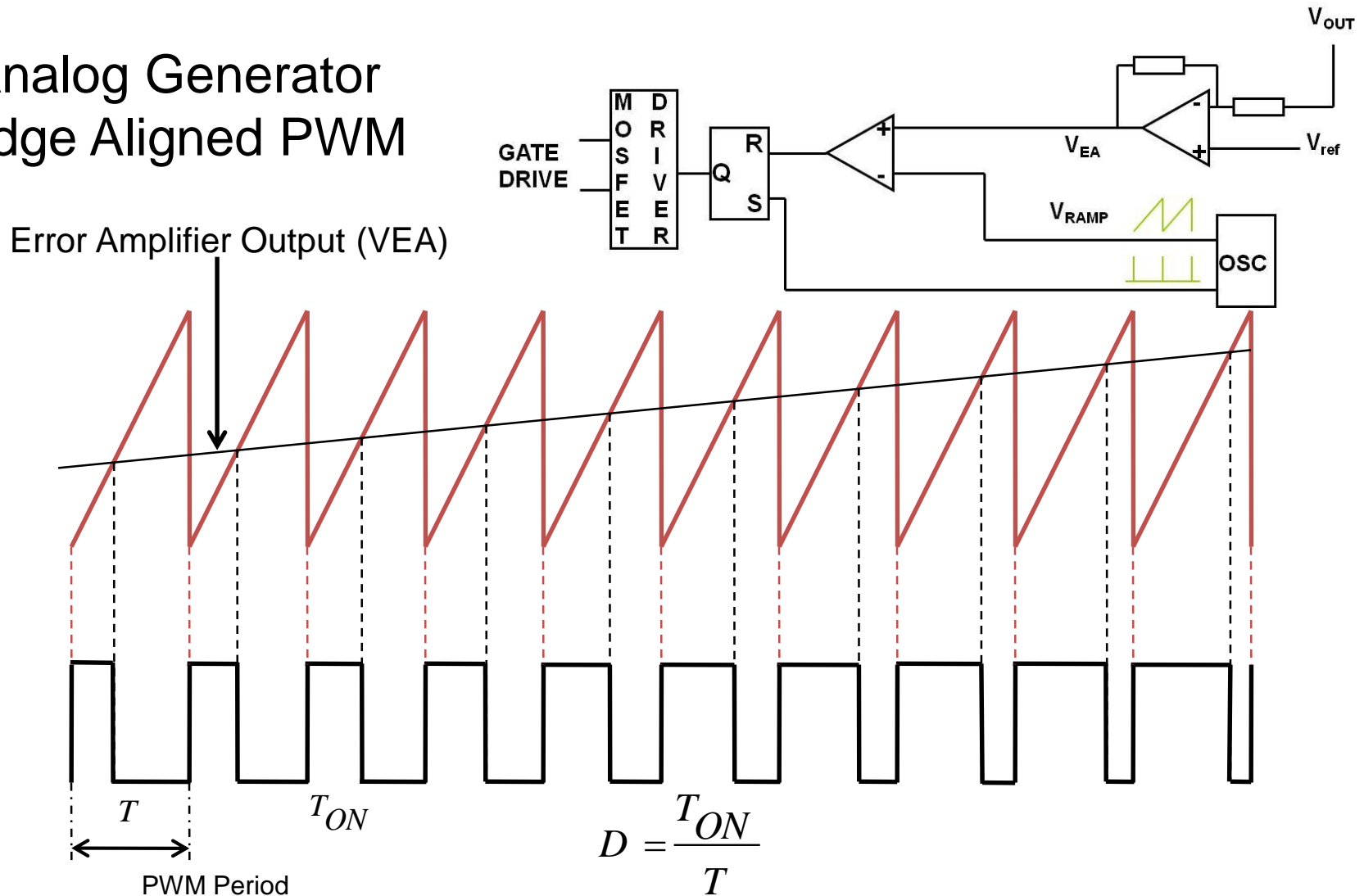
# Analog PWM SMPS Implementation



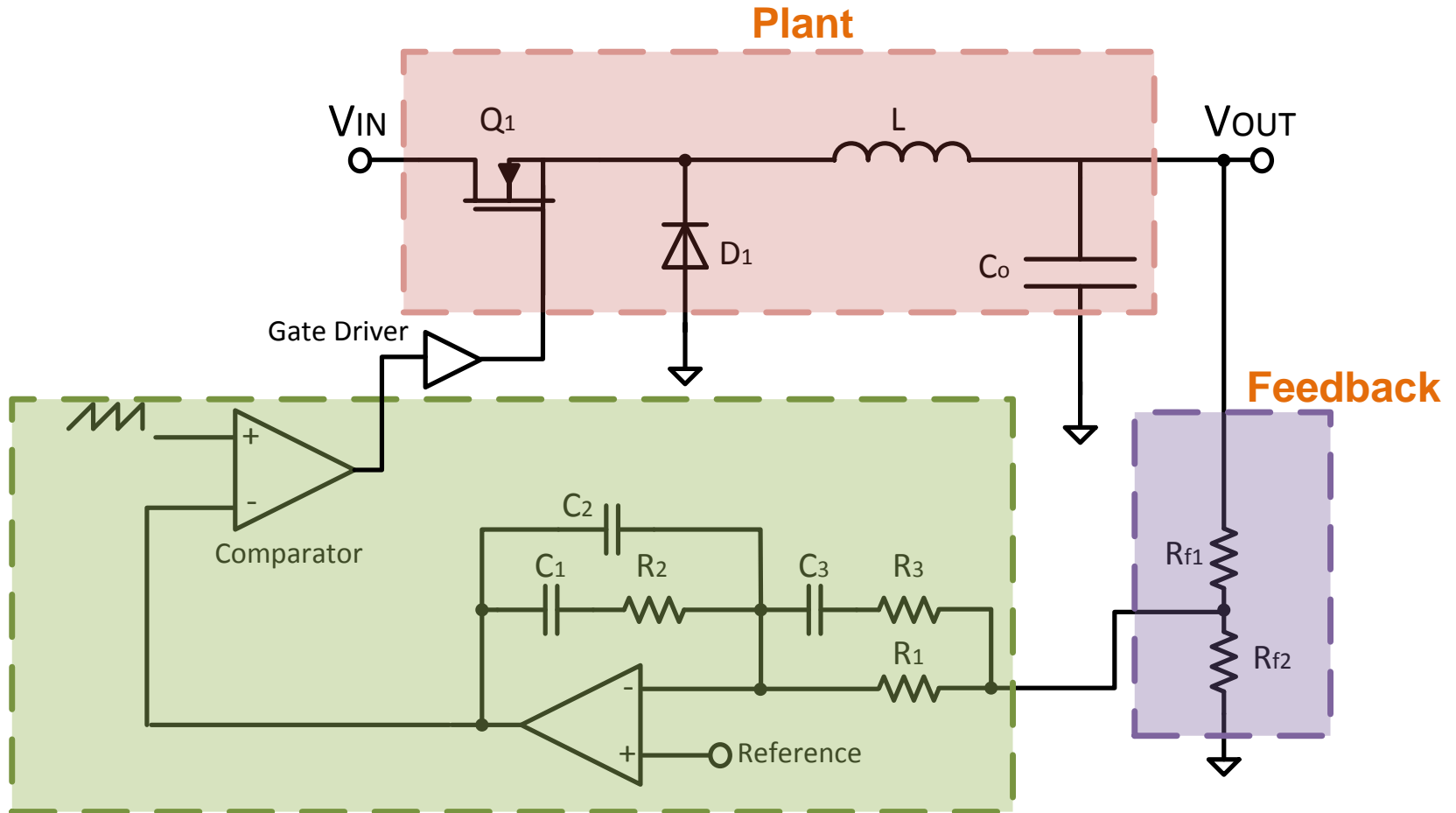
Analog Type III Compensator + PWM

# Analog PWM Generator

## Analog Generator Edge Aligned PWM

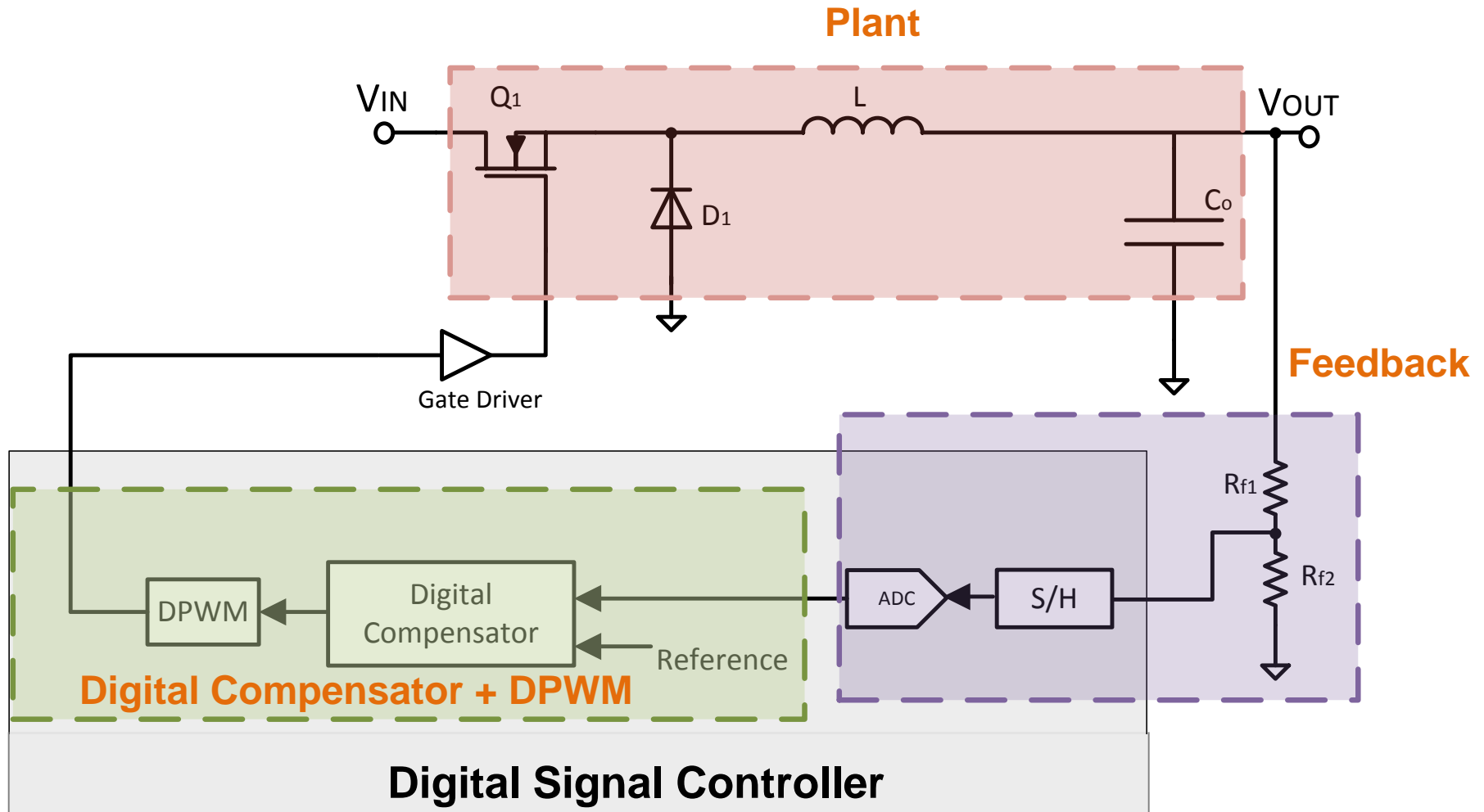


# Analog PWM SMPS Implementation

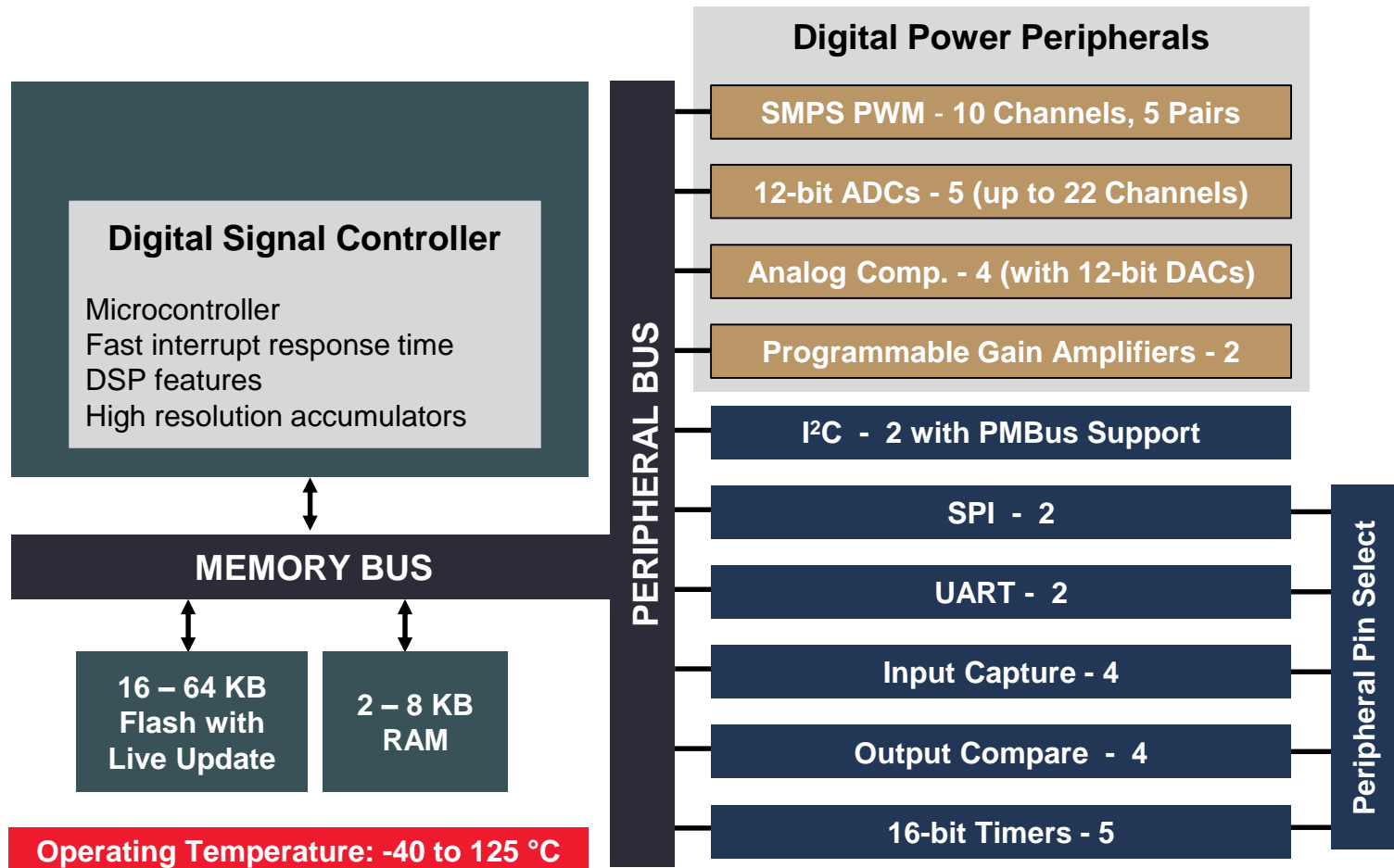


Analog Type III Compensator + PWM

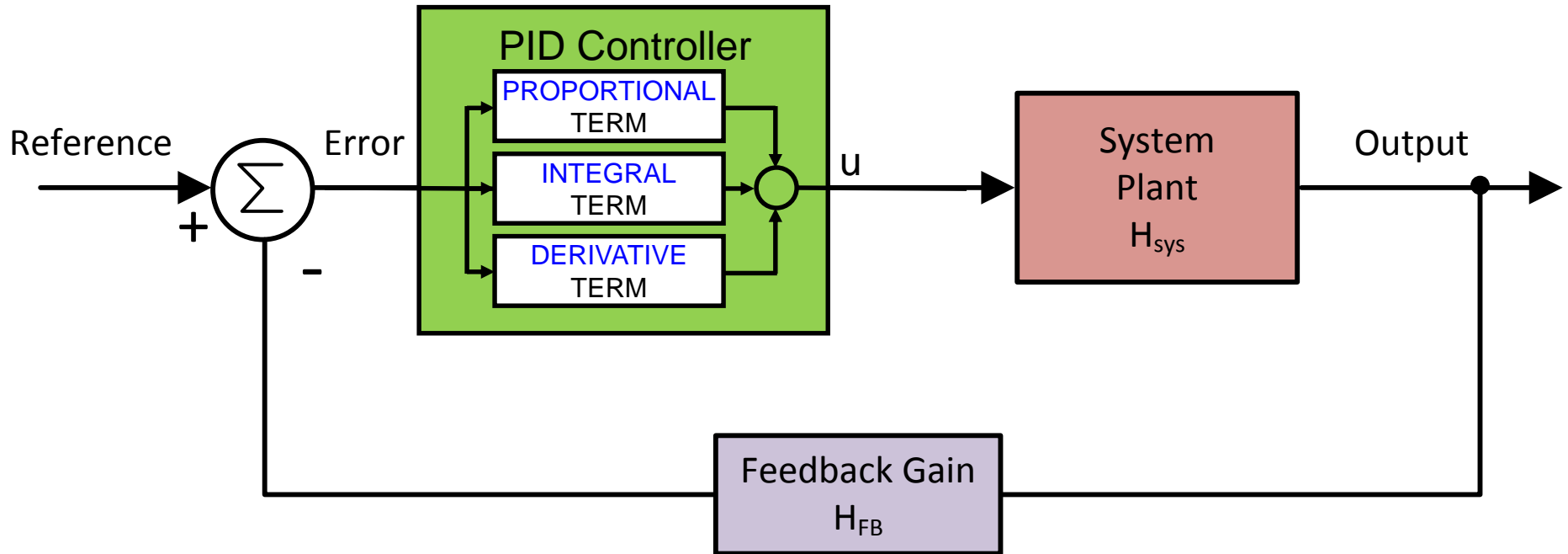
# Digital PWM SMPS Implementation



# Example Digital Signal Controller for Digital Power



# The PID Controller





# PID Controller Mathematics

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## PID Implementation

- From:  $R_{PID}^{BE}(s) = k_p + \frac{k_i}{s} + k_d s$

# PID Controller Mathematics

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## PID Implementation

- From:  $R_{PID}^{BE}(s) = k_p + \frac{k_i}{s} + k_d s$
- Using:  $s = \frac{z-1}{Tz}$  (Backward Euler)

# PID Controller Mathematics

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## PID Implementation

- From:  $R_{PID}^{BE}(s) = k_p + \frac{k_i}{s} + k_d s$
  - Using:  $s = \frac{z-1}{Tz}$  (Backward Euler)
  - We get: 
$$R_{PID}^{BE}(z) = \frac{\left(k_p + k_i T + \frac{k_d}{T}\right) + \left(-k_p - 2\frac{k_d}{T}\right)z^{-1} + \left(\frac{k_d}{T}\right)z^{-2}}{(1 - z^{-1})}$$
-

# PID Controller Mathematics

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## PID Implementation

Z-Domain:

$$R_{PID}^{BE}(z) = \frac{\left(k_p + k_i T + \frac{k_d}{T}\right) + \left(-k_p - 2\frac{k_d}{T}\right)z^{-1} + \left(\frac{k_d}{T}\right)z^{-2}}{(1 - z^{-1})}$$

Time  
Domain:

$$u(n) = u(n-1) + \left(k_p + k_i T + \frac{k_d}{T}\right)e(n) + \left(-k_p - 2\frac{k_d}{T}\right)e(n-1) + \left(\frac{k_d}{T}\right)e(n-2)$$

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# PID Controller Mathematics

## PID Implementation

Z-Domain:

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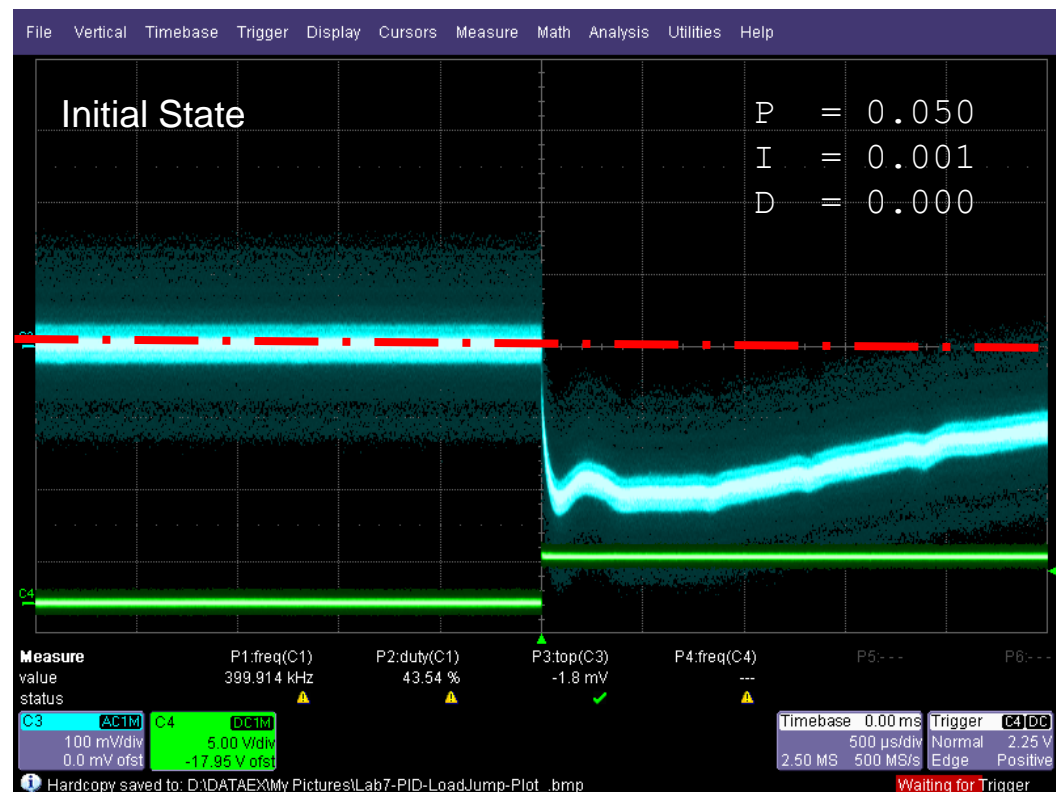
Time  
Domain:

$$u(n) = u(n-1) + \overset{K_A}{\left(k_p + k_i T + \frac{k_d}{T}\right)} e(n) + \overset{K_B}{\left(-k_p - 2\frac{k_d}{T}\right)} e(n-1) + \overset{K_C}{\left(\frac{k_d}{T}\right)} e(n-2)$$

Constants

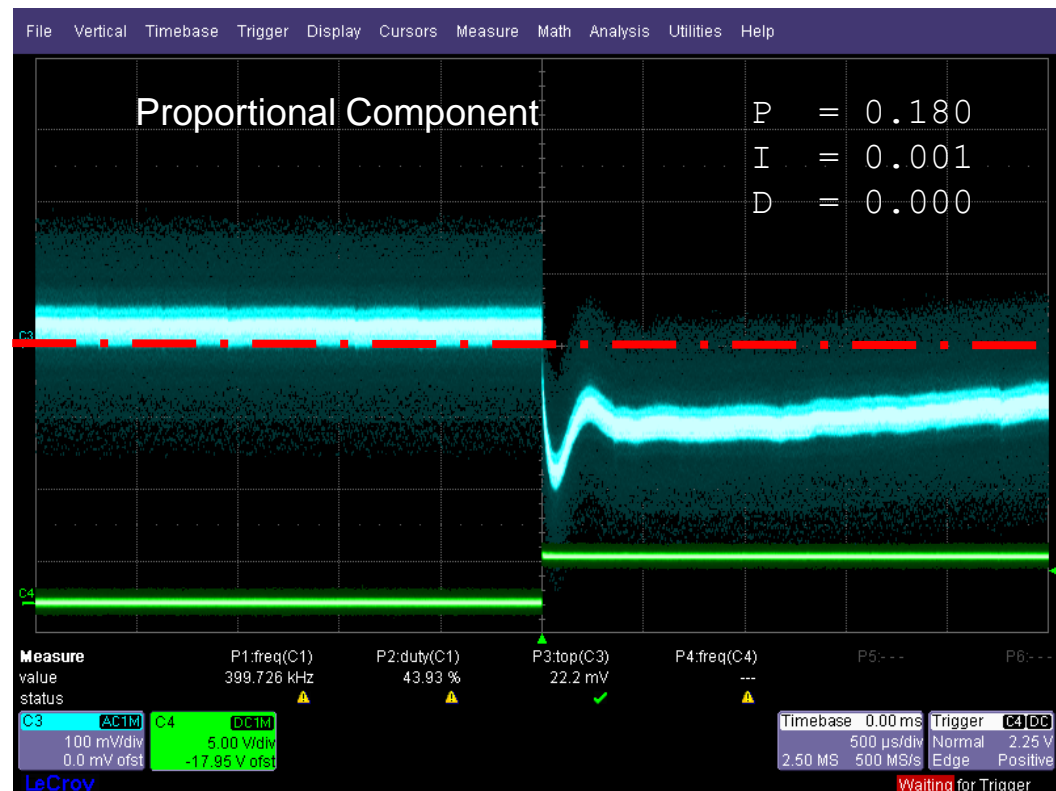
# Finding PID Coefficients Ziegler-Nichols Method

- 1) Start with  $K_P$  and  $K_I$  coefficients near to (but not) zero. ( $K_D$  can be 0)
- 2) Allow system to stabilize, then introduce a step change in the load



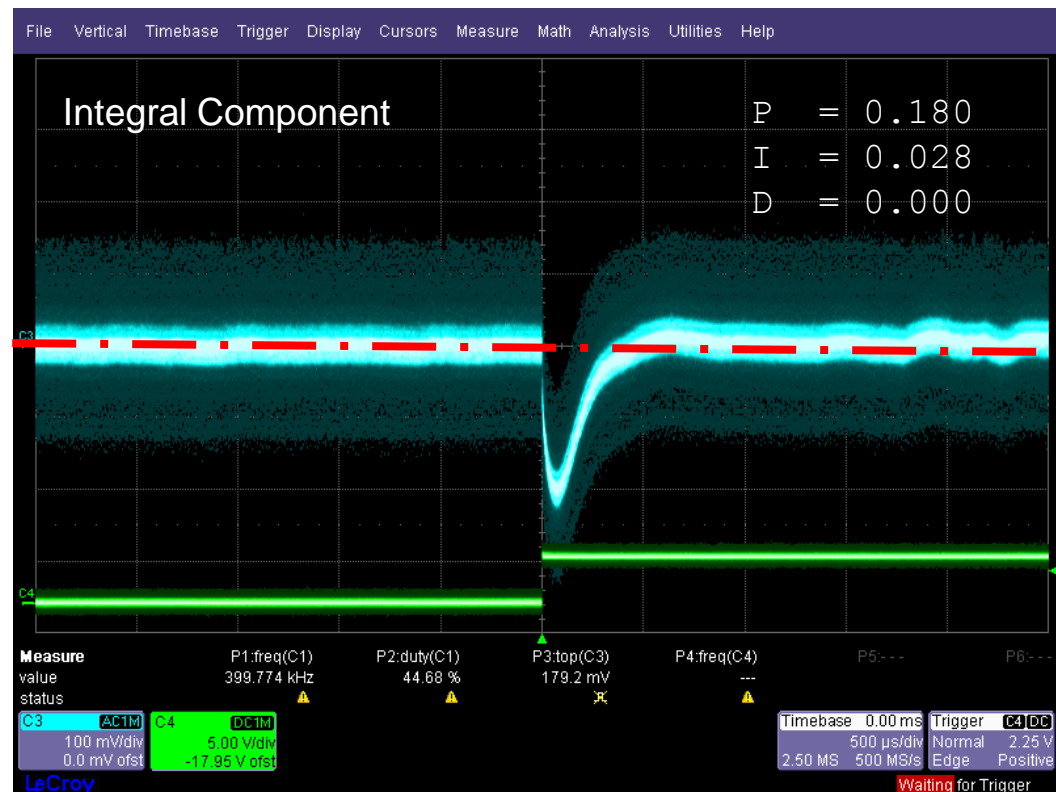
# Finding PID Coefficients Ziegler-Nichols Method

- 3) Increase  $K_P$  until the tiny overshoot reaches the output voltage level and then reduce it to approx. 70% of its value



# Finding PID Coefficients Ziegler-Nichols Method

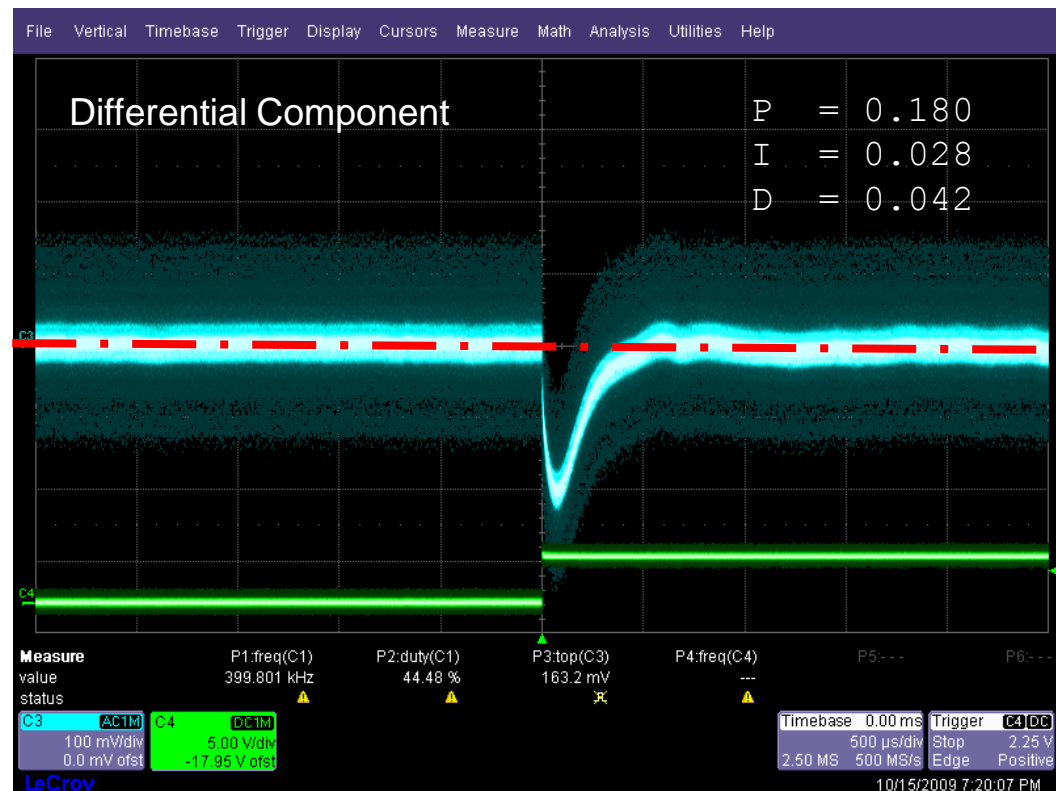
4) Increase  $K_I$  to get a nice response





# Finding PID Coefficients Ziegler-Nichols Method

- 5) Increase  $K_D$  reduce oscillations during the load-condition  
(Keep  $K_D$  low to avoid noise susceptibility)



# PID Controller Mathematics

## PID Implementation

Z-Domain:

$$R_{PID}^{BE}(z) = \frac{\left(k_p + k_i T + \frac{k_d}{T}\right) + \left(-k_p - 2\frac{k_d}{T}\right)z^{-1} + \left(\frac{k_d}{T}\right)z^{-2}}{(1 - z^{-1})}$$

Time  
Domain:

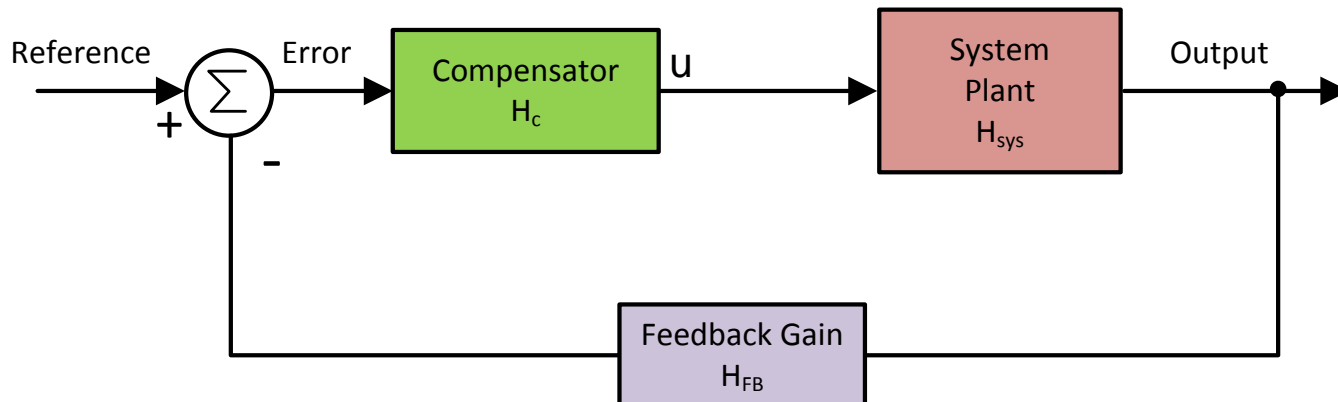
$$u(n) = u(n-1) + \overset{K_A}{\left(k_p + k_i T + \frac{k_d}{T}\right)} e(n) + \overset{K_B}{\left(-k_p - 2\frac{k_d}{T}\right)} e(n-1) + \overset{K_C}{\left(\frac{k_d}{T}\right)} e(n-2)$$

Constants

# Finding the Coefficients Using a Model

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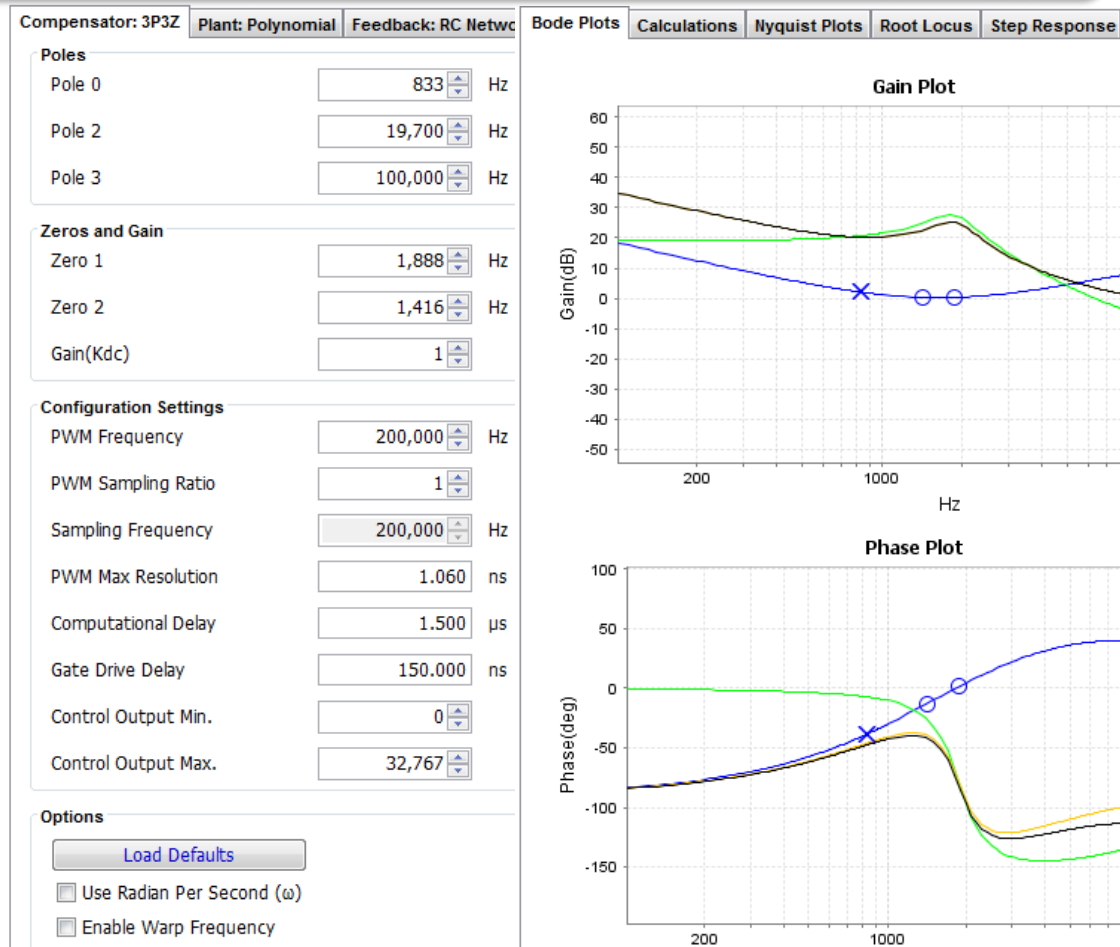
- Circuitry can be modeled and coefficients calculated using simulation tools like MATLAB
- Characterize power circuitry to get equation for the system plant output in terms of the controlled variable ( $u$ )
- The compensator equation is known – an output of the controlled variable ( $u$ ) in terms of the process output
- Substitute the process equation into the compensator equation and solve for the coefficients using simultaneous equations



# Finding the Coefficients Using a Tool - DCDT

Eliminate the need for manual bi-linear transform calculations

- **Input Plant Details**
  - Polynomial or Pole/Zero form
  - Imported data table from simulation or network analyzer
- **Five Compensator Types**
  - Digital 2P2Z, Digital 3P3Z
  - PID, Analog Type II, III
- **Generate header file with compensator coefficients**
- **Analyze response & stability**



# PID Controller Mathematics

## PID Implementation

Z-Domain:

$$R_{PID}^{BE}(z) = \frac{\left(k_p + k_i T + \frac{k_d}{T}\right) + \left(-k_p - 2\frac{k_d}{T}\right)z^{-1} + \left(\frac{k_d}{T}\right)z^{-2}}{(1 - z^{-1})}$$

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Constants

# MAC Instruction

One instruction,  
One clock cycle,  
8 operations

MAC  $w6 * w7, A, [w8] += 2, w6, [w10] -= 4, w7, [w13] += 2$

One instruction performs:

$A = W6 * W7$  ;  $W6$  multiplied by  $W7$  and product added to  $A$

$W6 = (W8)$  ; load new data addressed by  $W8$  into  $W6$

$W7 = (W10)$  ; load new data addressed by  $W10$  into  $W7$

$W8 = W8 + 2$  ; Add 2 to address in  $W8$

$W10 = W10 - 4$  ; Subtract 4 from address in  $W10$

$(W13) = B$  ; Copy  $B$  (rounded) to memory specified by  $W13$

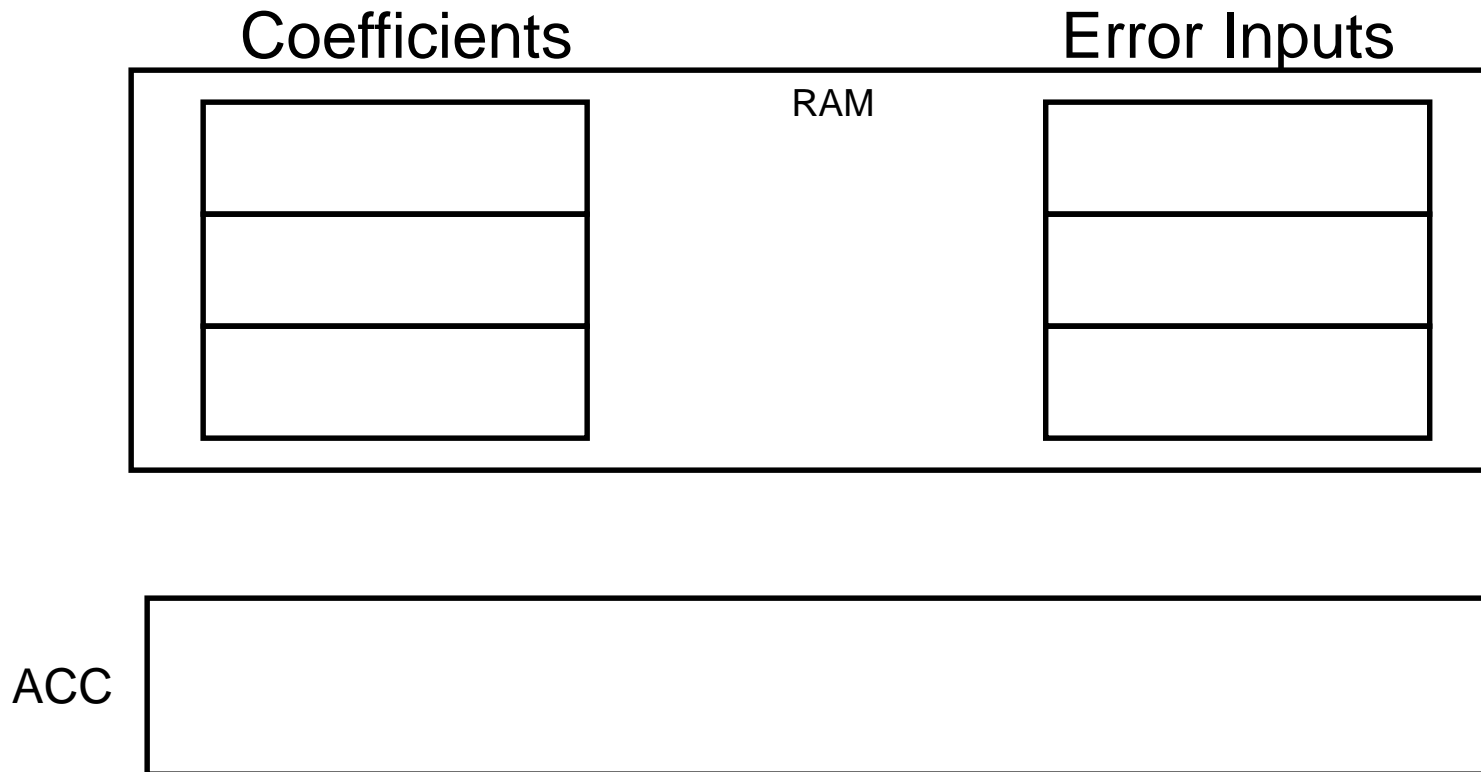
$W13 = W13 + 2$  ; Increment  $W13$  by 2

One  
instruction,  
One clock  
cycle

# DSC Digital PID

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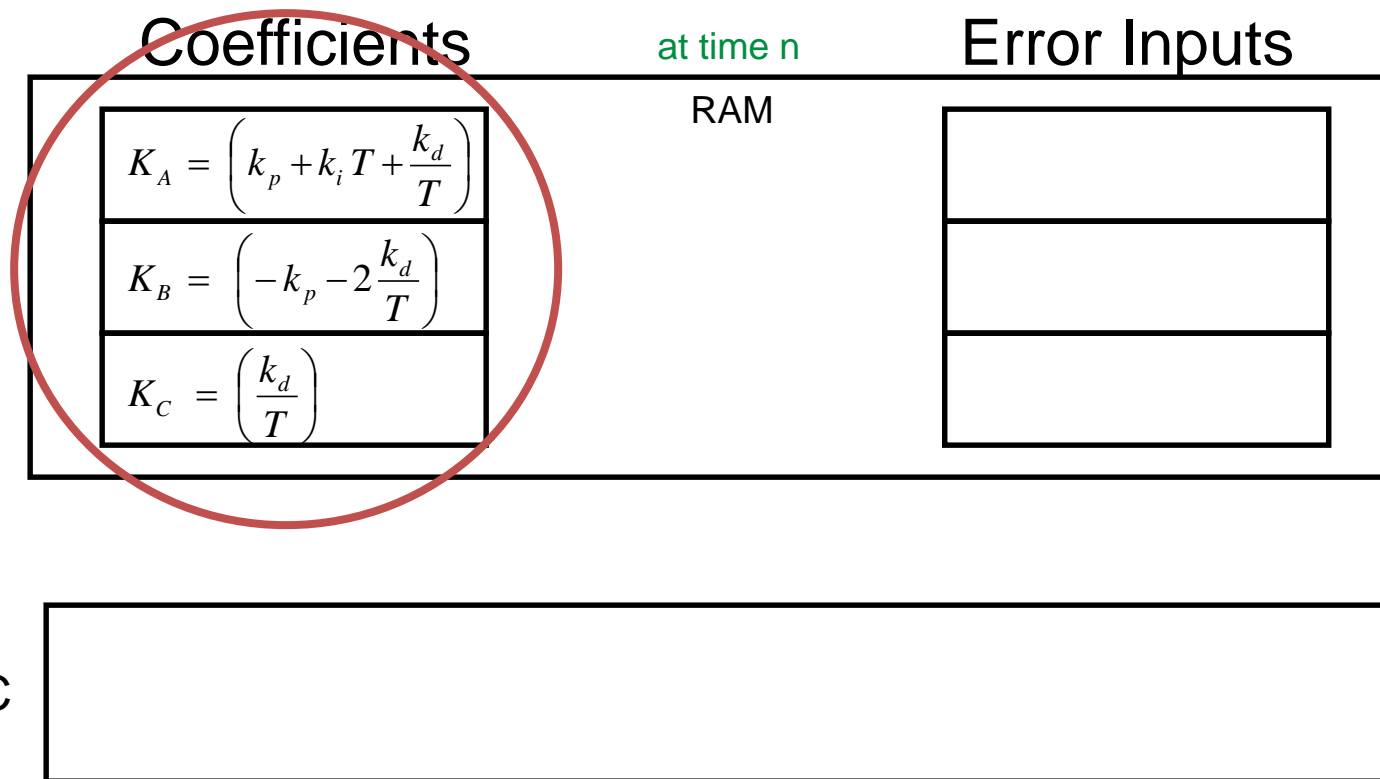
## PIDs in DSCs: Architecture



# DSC Digital PID

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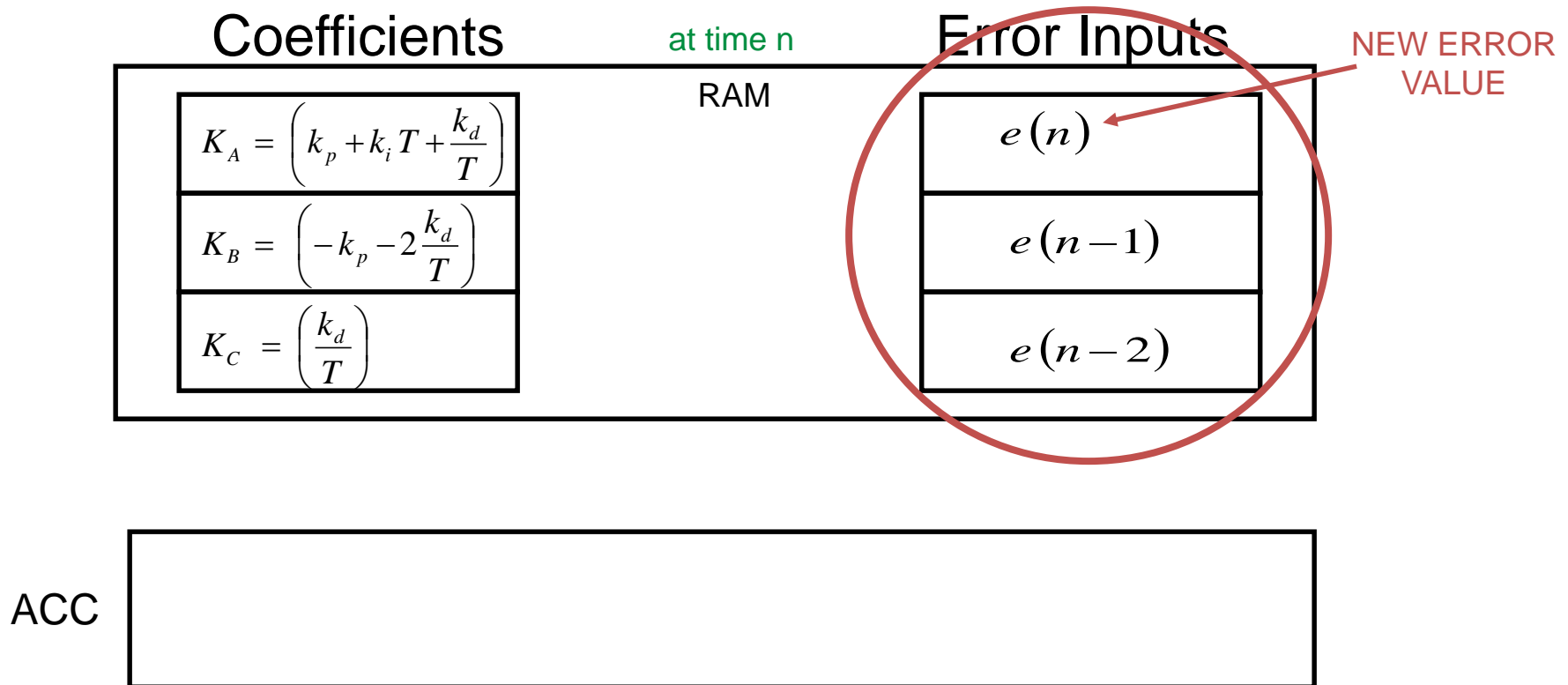
## PIDs in DSCs: Coefficients





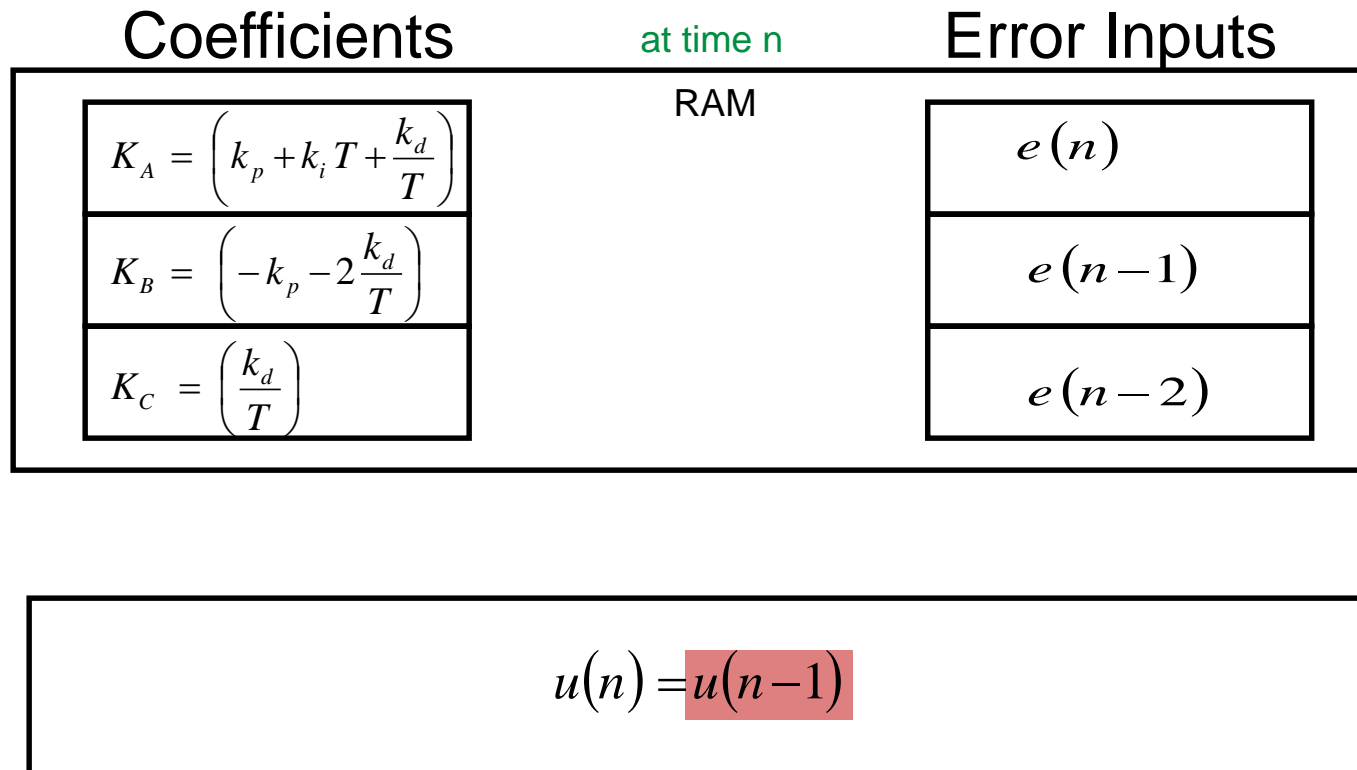
# DSC Digital PID

## PIDs in DSCs: New Error Value



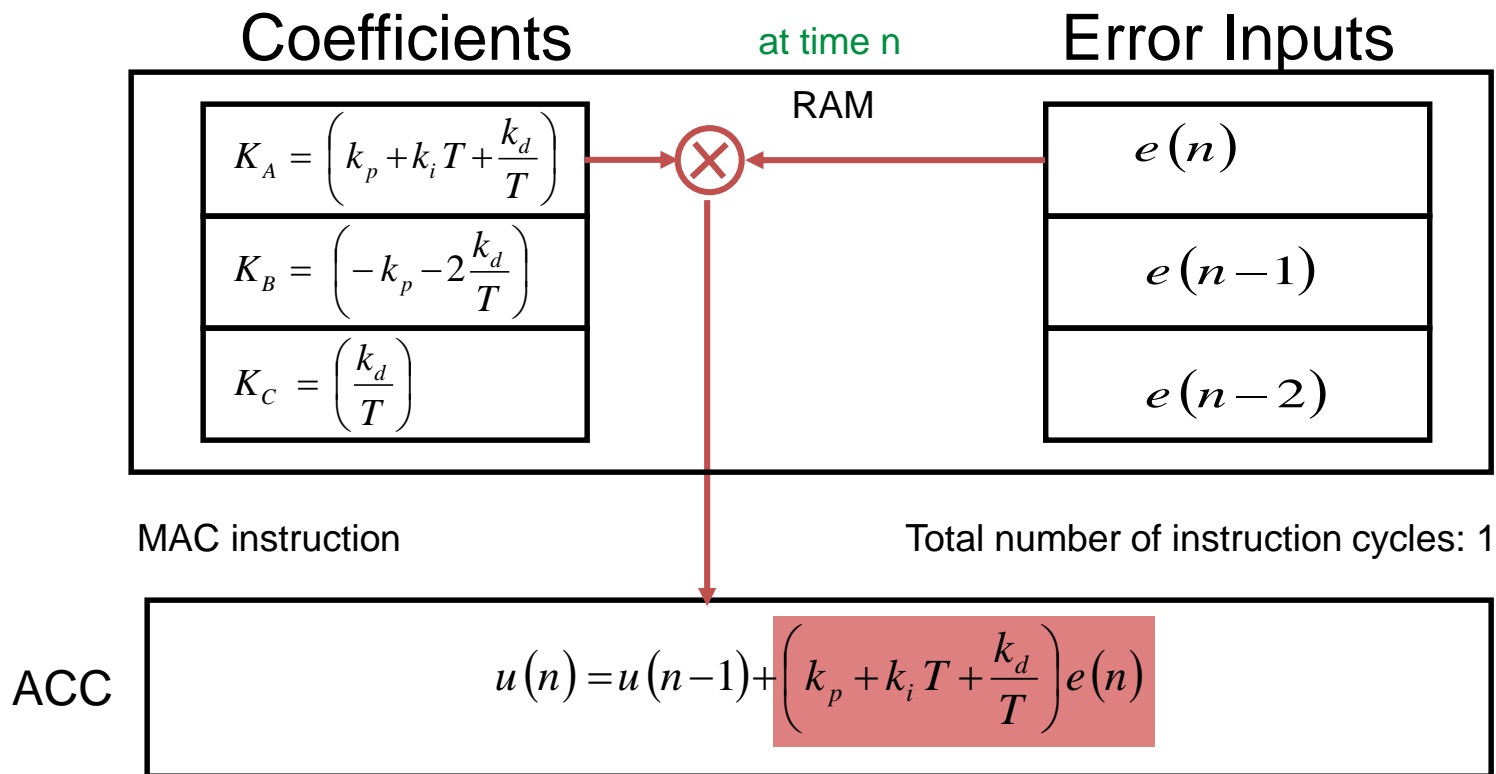
# DSC Digital PID

## PIDs in DSCs: Previous result



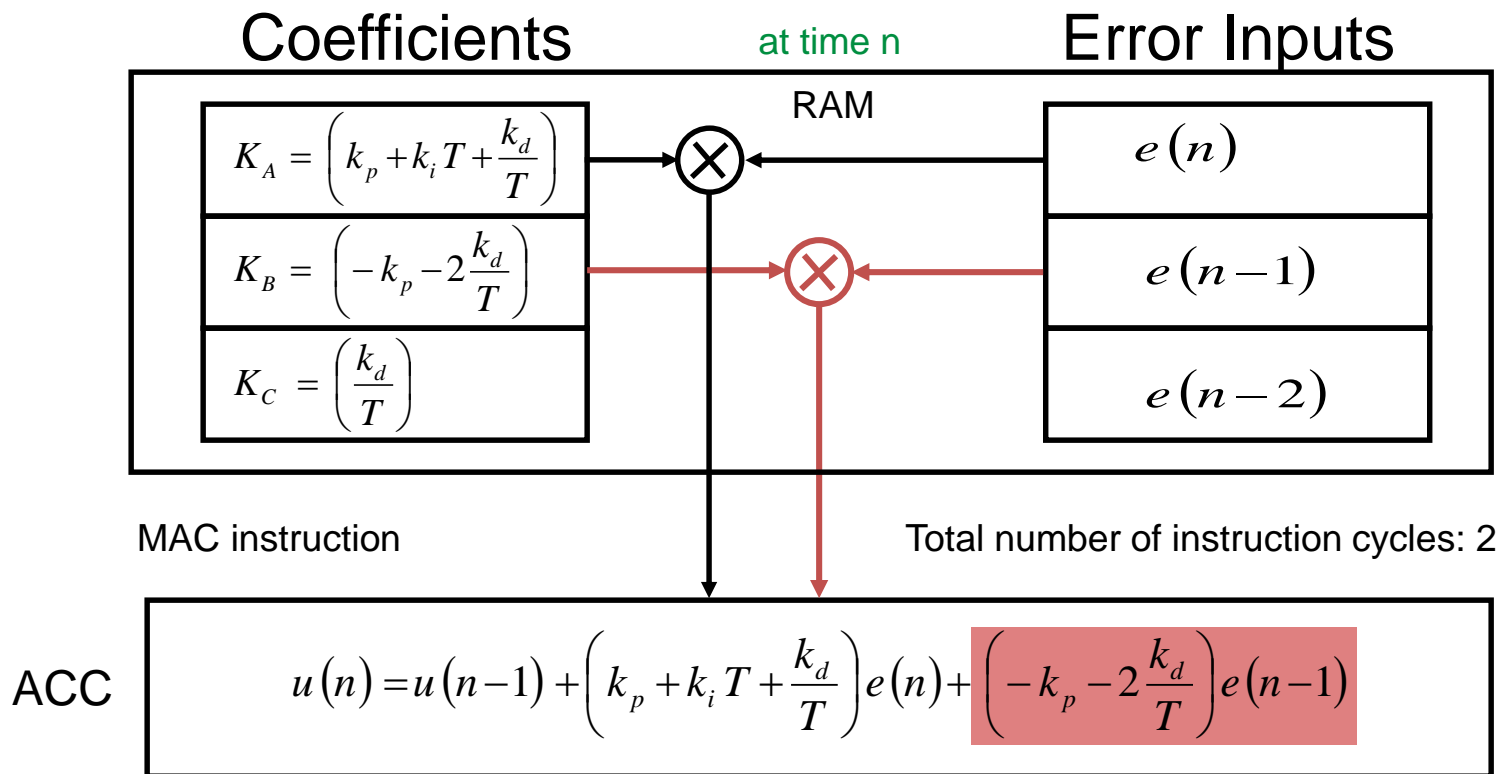
# DSC Digital PID

## PIDs in DSCs: First Contribution



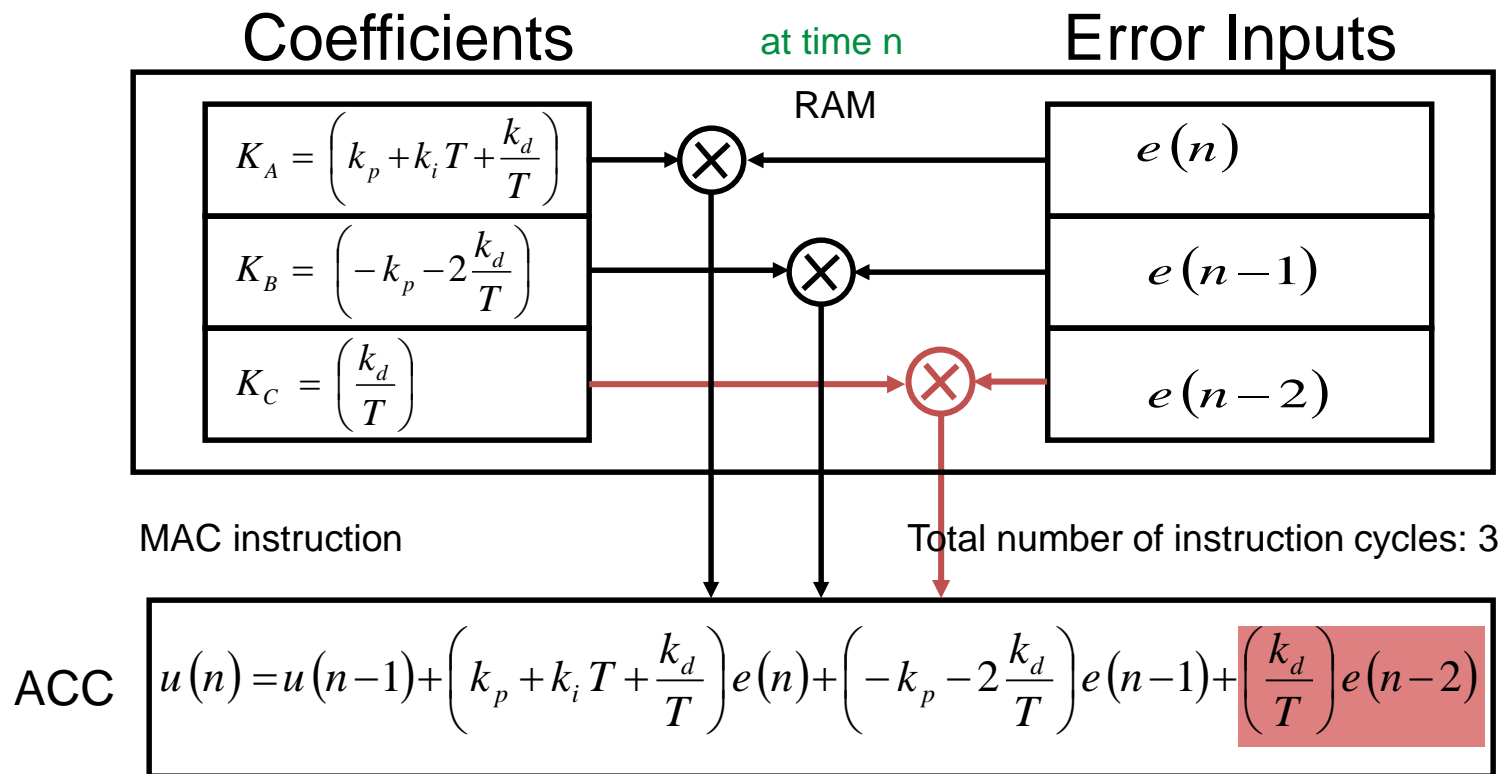
# DSC Digital PID

## PIDs in DSCs: Second Contribution



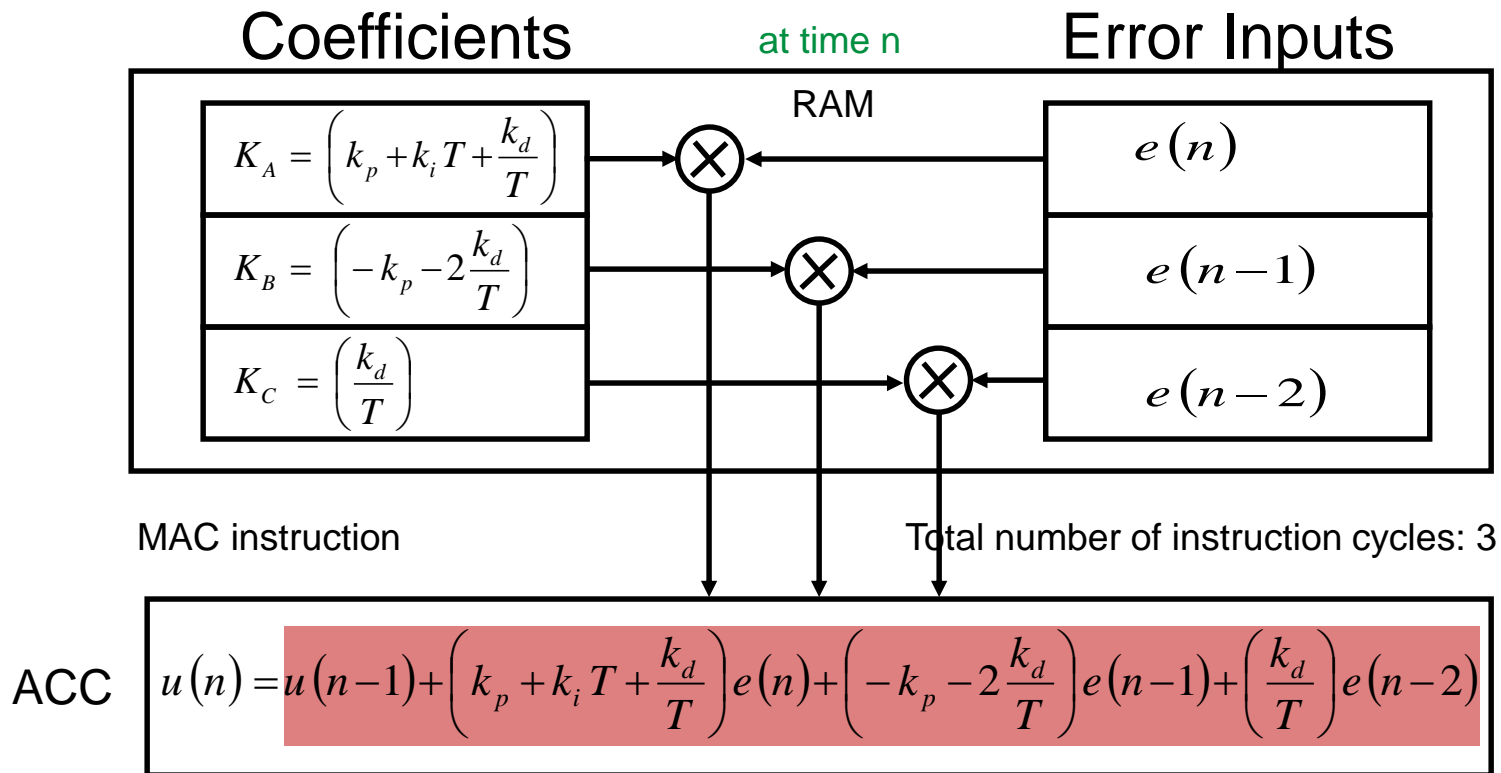
# DSC Digital PID

## PIDs in DSCs: Third Contribution



# DSC Digital PID

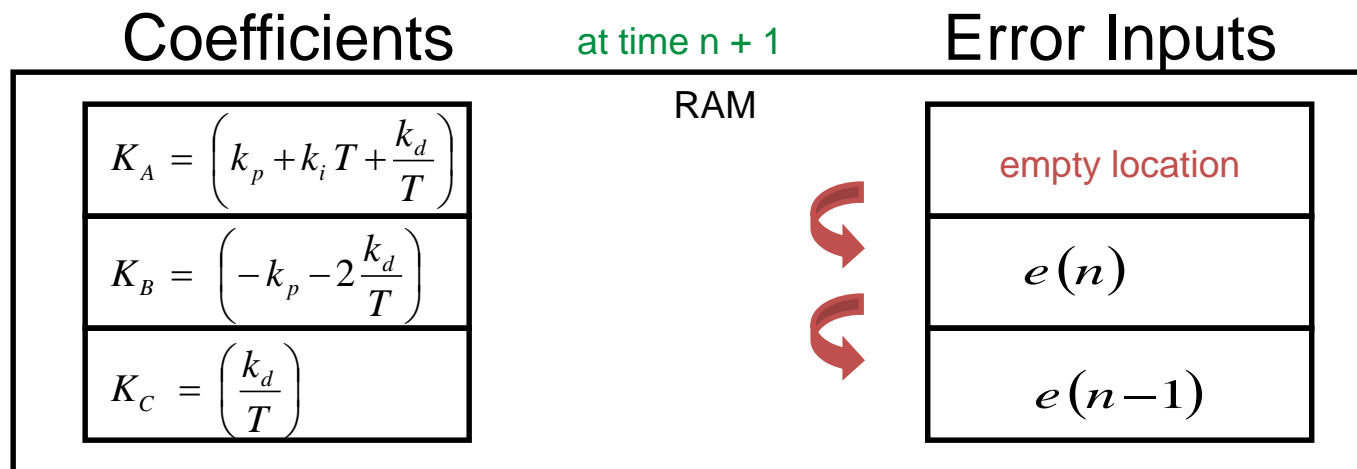
## PIDs in DSCs: Updated result



**Digital PID Equation**

# DSC Digital PID

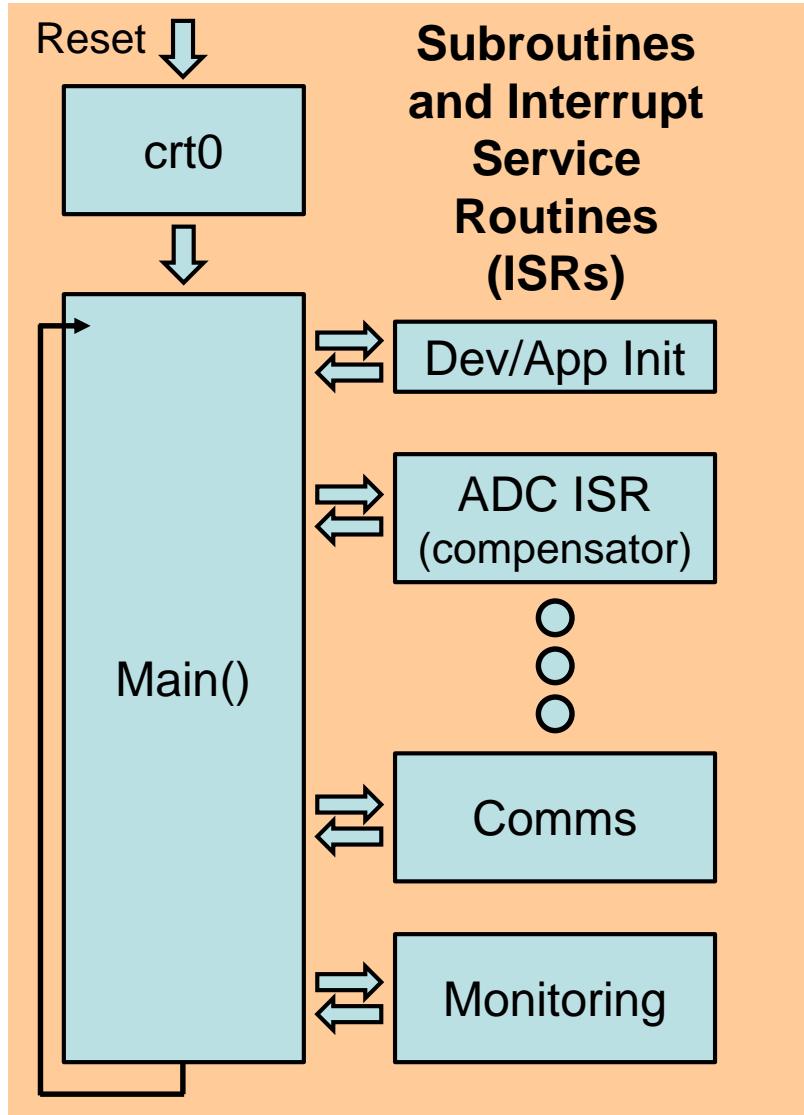
## PIDs in DSCs: Ready for Next Iteration



ACC

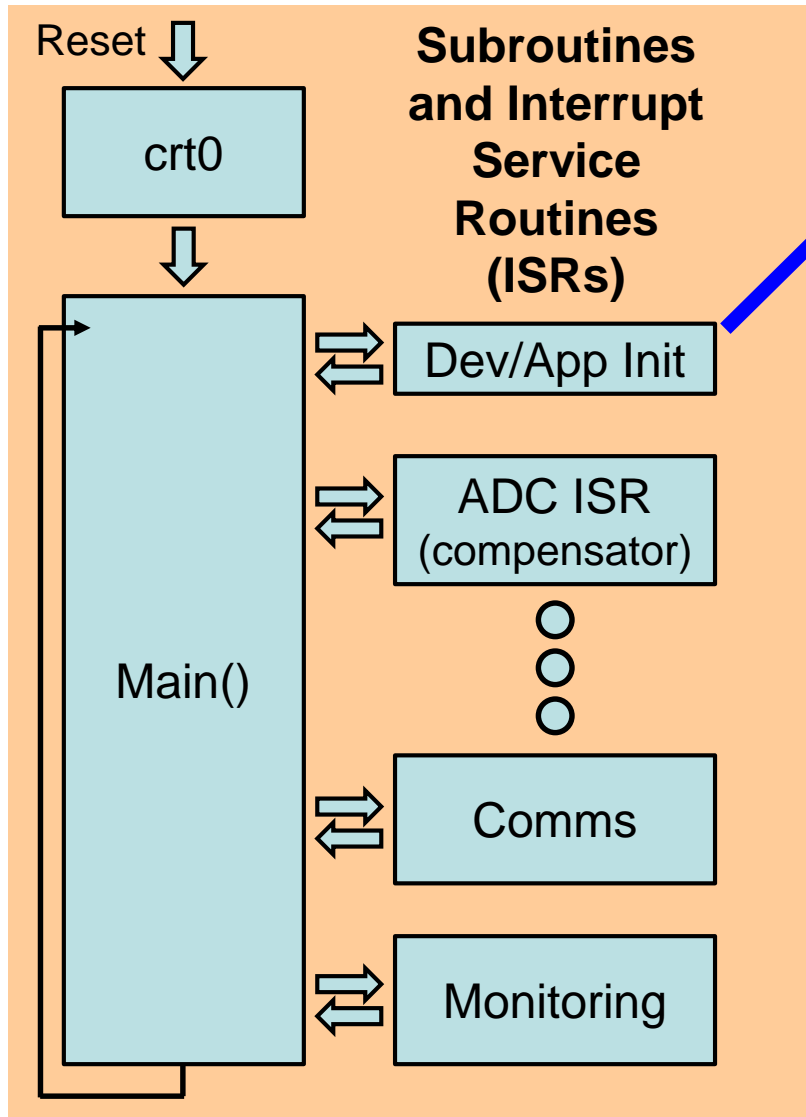
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# Typical DSC Firmware Architecture





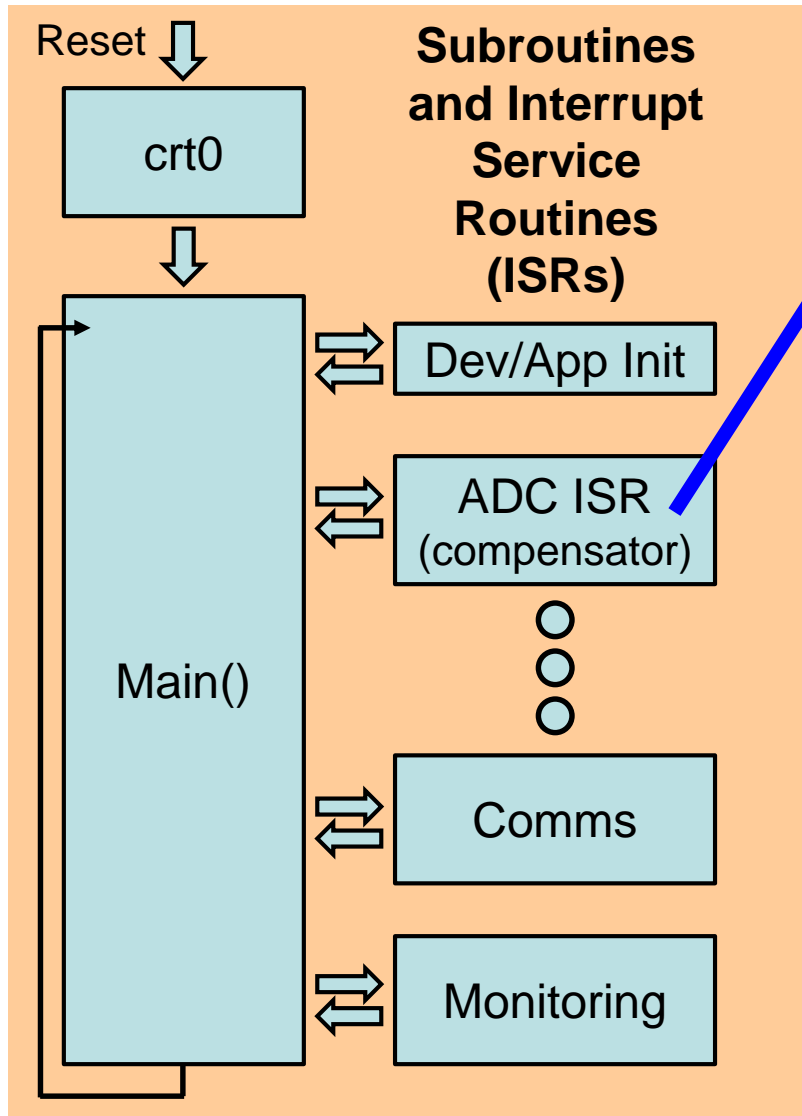
# Typical DSC Firmware Architecture



## Device / Application Initialization

`InitClock();` Setup DSC oscillator and clock  
`InitComp();` Setup current limit comparator  
`InitADC();` Setup ADC for output voltage sampling  
`InitPWM();` Setup PWM  
`InitIO();` Setup I/O  
`InitPID();` Initialize compensator, setup pointers, clear error and output history

# Typical DSC Firmware Architecture

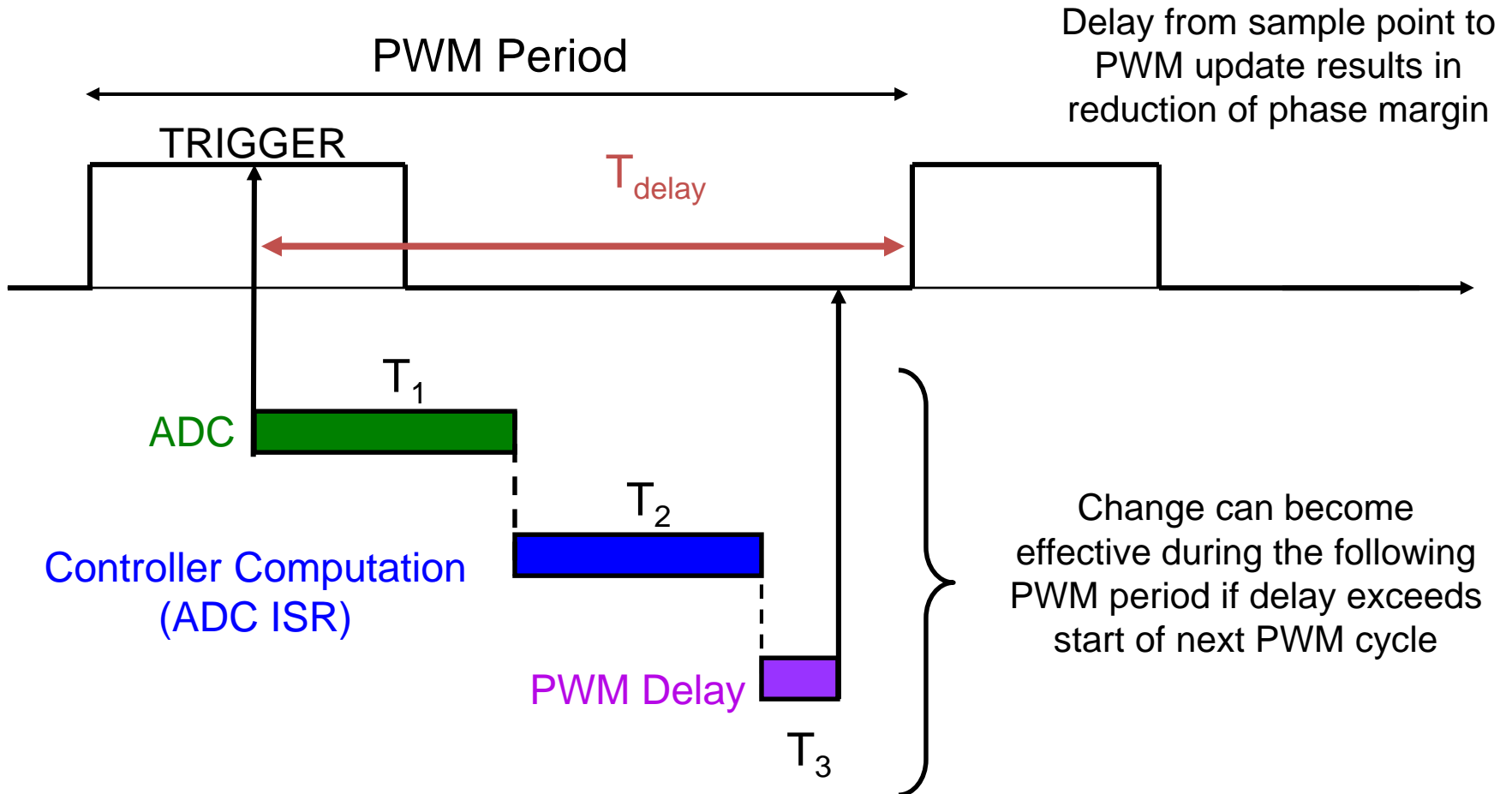


## ADC Interrupt – The Compensator

- Clear interrupt flag
- Init pointers to coefficients and errors arrays
- Read new voltage sample value
- Scale the input voltage
- Computation of  $e(n) = V_{ref} - \text{input voltage}$
- Voltage mode PID computation
- Update the voltage error history
- Check if duty cycle is within limits
- If needed, clamp to min or max value
- Save new PWM duty cycle value in register

# Control Loop Timing

## Digital Implementation of a Control Loop

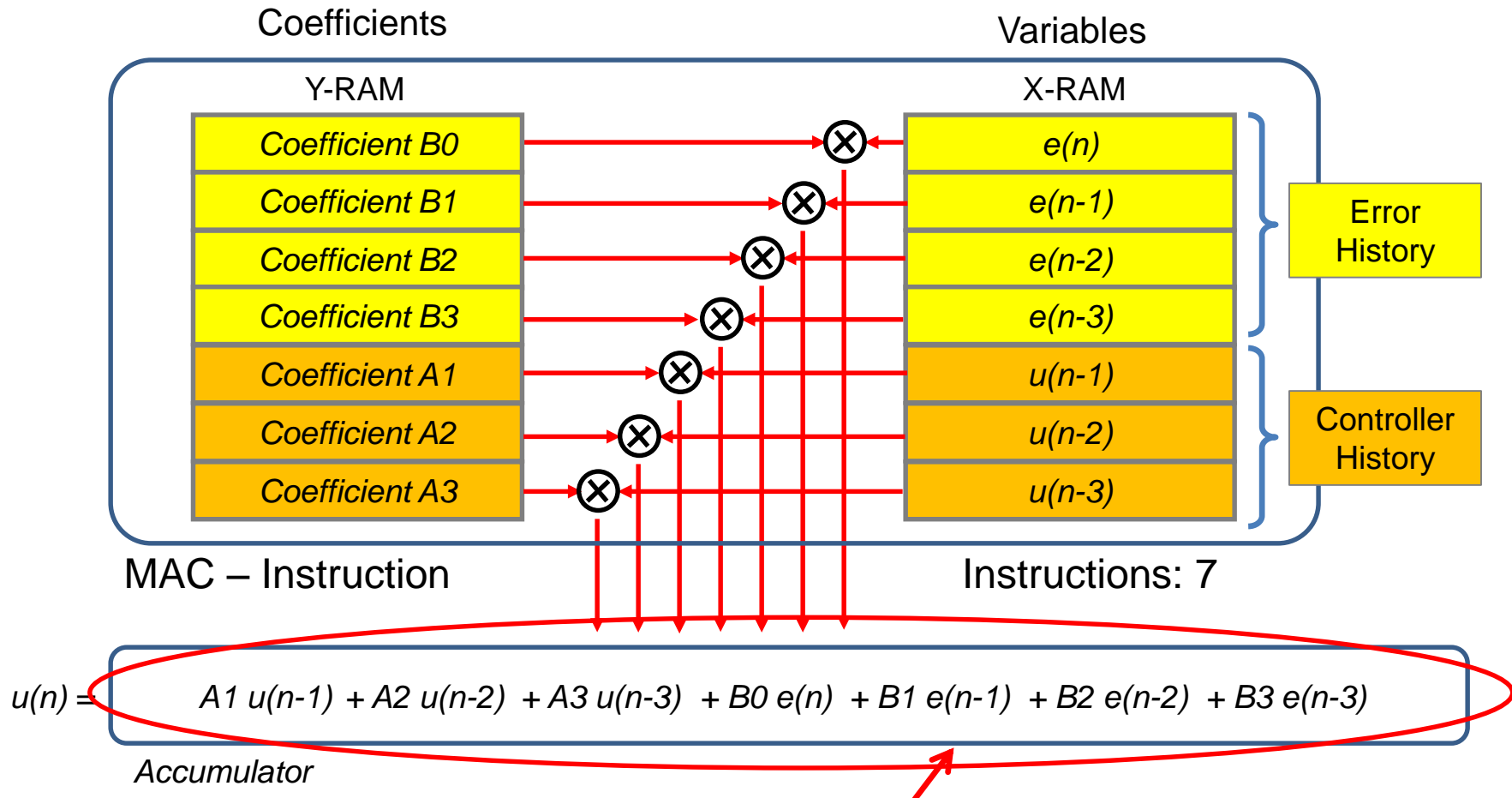


# Digital Compensator Types

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- **Proportional Integral Derivative (PID)**
    - Most common compensator type in industrial control applications, although not ideal for SMPS applications
    - Uses only three coefficients – simple method to find the values
    - Only compensates one pole and one zero of plant
  - **Digital 2P2Z (similar to Analog Type II)**
    - Five coefficients – Five MAC instructions to calculate
    - Current-mode converters
  - **Digital 3P3Z (similar to Analog Type III)**
    - Seven coefficients – Seven MAC instructions to calculate
    - Voltage-mode buck or boost-derived converters
-

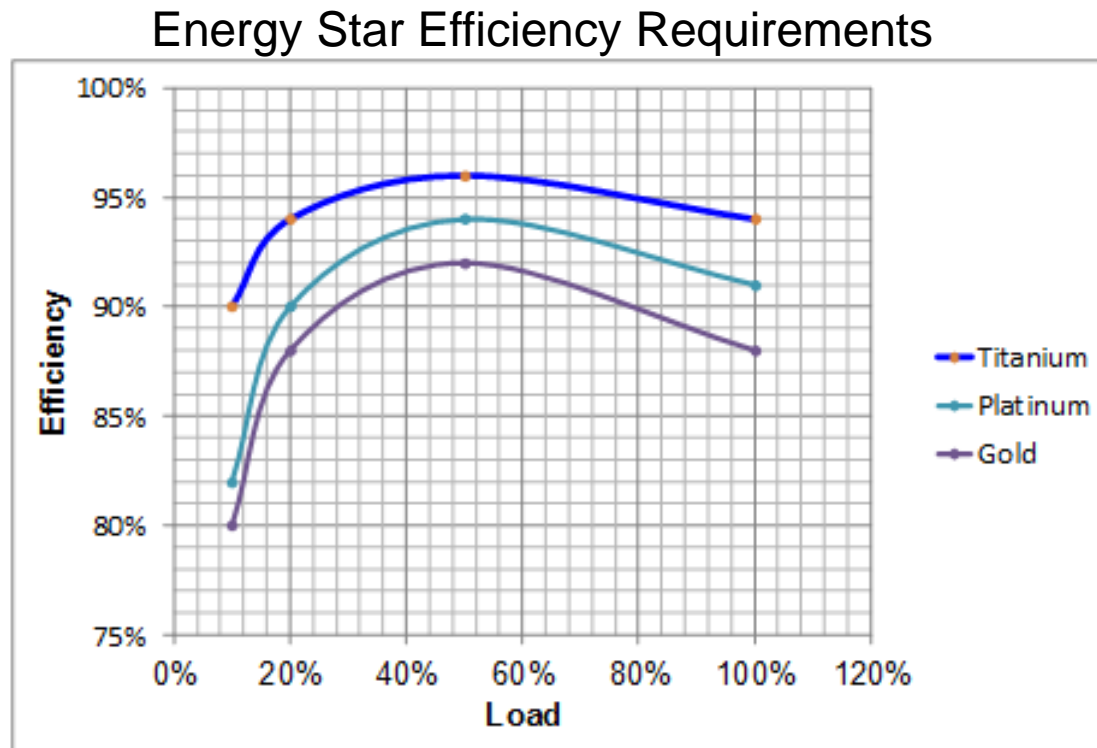
# Linear Difference Equation for 3P3Z Compensator



Linear difference equation of a digital type III (3p3z) compensator

# Full Digital Control Adaptive Algorithms

- Improving Efficiency over widely varying loads
  - Phase shedding
  - Dead-time adjustment
  - Variable switching frequency
  - Variable bulk voltage

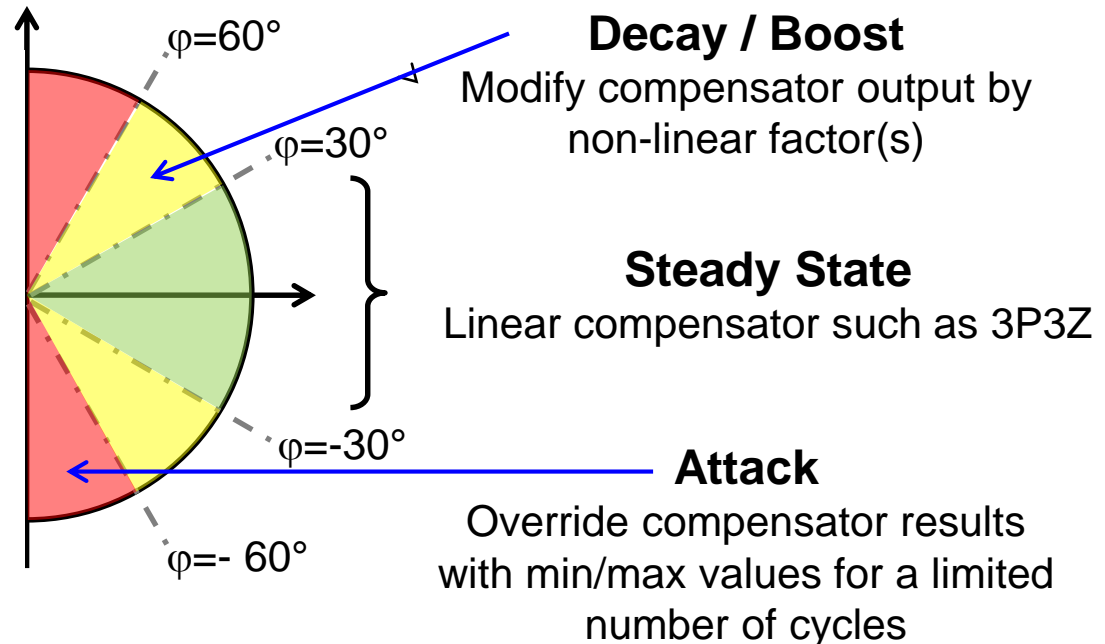


# Full Digital Control Predictive and Non-linear Algorithms

- **Dynamic Responsiveness**

- Non-linear Algorithms
  - Real-time coefficient scaling
- Predictive Algorithms
  - Bypass damping of control loops

$\phi$  represents a vector:  
Sum of the absolute  
value of 3 error samples  
vs 0 degree vector  
representing errors  
averaging zero



# SMPS Application Notes / Guides

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- **DS70336 – Buck/Boost Converter PICtail User Guide**
  - **AN1114 – Switch Mode Power Supply Topologies (Part I)**
  - **AN1207 – Switch Mode Power Supply Topologies (Part II)**
  - **AN1106 – Power Factor Correction**
  - **DS70320 – dsPIC SMPS AC-DC Reference Design User Guide**
  - **AN1278 – Interleaved Power Factor Correction**
  - **AN1279 – 1000VA Off-line UPS**
  - **AN1335 – Quarter Brick PSFB DC/DC**
  - **AN1336 – LLC DC/DC**
  - **AN1338 – Grid-Connected Solar Micro-Inverter**
-



# SMPS Compensator Libraries

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- 3P3Z, 2P2Z, and PID Compensators
    - Good compromise between speed vs. resolution
    - 3P3Z takes ~ 1.6us, 2P2Z takes ~1.4us
  - Compensators written to support MATLAB code generation (future)
    - MATLAB needs specific Inputs and Outputs to be defined
    - `void SMPS_Controller3P3ZUpdate(SMPS_3P3Z_T* controllerData, volatile uint16_t* controllerInputRegister, int16_t reference, volatile uint16_t* controllerOutputRegister);`
      - Pointer to structure (min/max clamps, pre/post shifts, coefficients, and control/error history)
      - Pointer to control input (i.e. ADCBUFx)
      - Control Reference
      - Pointer to control output (PDCx, CMPDACx, etc.)
-

# Microchip / Biricha

## Digital Power Workshops

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**Microchip has teamed up  
with Biricha Digital Power  
to offer world-leading  
expertise and training in  
the field of digital power**

- **2015 Workshops:**

- Feb 10-12: Karlsruhe, Germany (€1400)
- Jun 2-4: Boston, Massachusetts (\$1400)
- Oct 6-8<sup>th</sup>: Stockholm, Sweden
- Oct 27-29<sup>th</sup>: San Jose, CA

**For More Information:**

[www.microchip.com/biricha](http://www.microchip.com/biricha)

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- **Day 1: Introduction to Digital Power Programming**

- Introduction to dsPIC33 family architecture and peripherals
- Device setup: Configuration of registers and the oscillator
- General Purpose: I/O ports, timers and interrupts
- Digital Power: PWM, comparator and analog to digital converter
- Introduction to MPLAB® X IDE and program/debug tools
- Fixed point math and number formatting
- Setting up the ADC module and using ADC interrupts

- **Day 2: Digital Power Supply Design**

- Detailed study of analog power supply design fundamentals
- Step-by-step digital power supply design
- Implementing a simple digital controller for your digital power supply
- Stable digital compensators for voltage mode control

- **Day 3: Digital Peak Current Mode Control**

- Detailed review of analog peak current mode design
- Sub-harmonic oscillations and slope compensation
- Digital peak current mode controller design
- High performance digital power supply design and implementation

# Review

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Product Marketing Manager,  
MCU16 Division,  
Microchip Technology, Inc.

Moderator:

Rich Nass,  
EVP, OpenSystems Media

## Audience Q & A via Chat

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MODULE ON YOUR SCREEN,  
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## Thanks for joining us



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E-mail us at:

[jgilmore@opensystemsmedia.com](mailto:jgilmore@opensystemsmedia.com)

